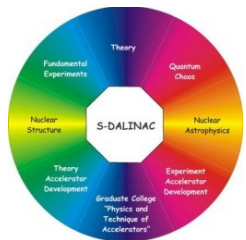


Three-body forces: From exotic nuclei to neutron stars

Achim Schwenk



TECHNISCHE
UNIVERSITÄT
DARMSTADT



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HELMHOLTZ
ASSOCIATION
Szymanski Prize
Warsaw, Nov. 17, 2015

Minerva
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Bundesministerium
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Nagroda imienia

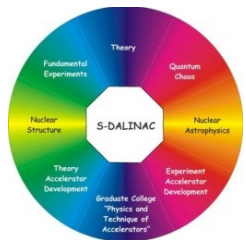
Zdzisława Szymańskiego

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Outline

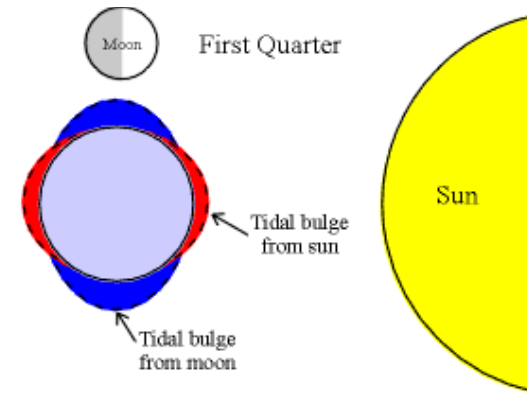
Understanding three-nucleon ($3N$) forces

$3N$ forces and neutron-rich nuclei

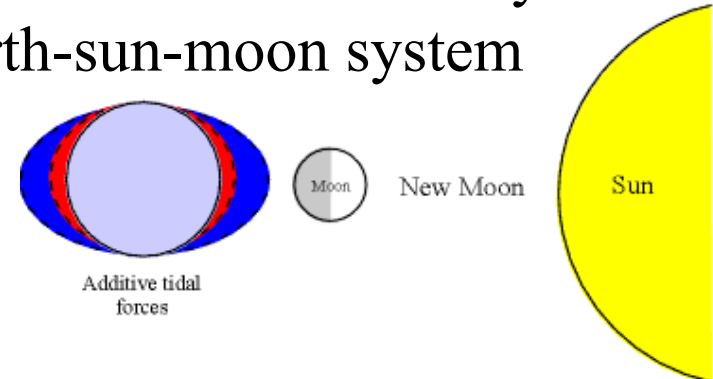
$3N$ forces and neutron matter/stars

Dark matter response of nuclei

Why are there three-body forces?



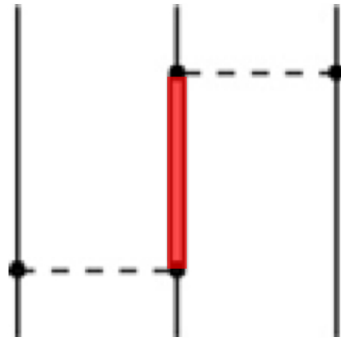
tidal effects lead to 3-body forces
in earth-sun-moon system



Why are there 3N forces?

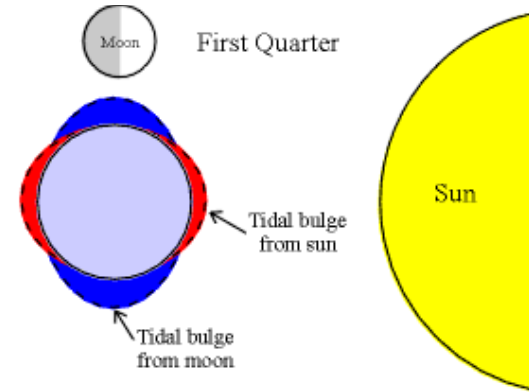
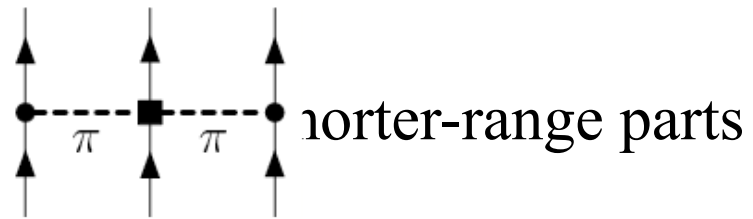
Nucleons are finite-mass composite particles,
can be excited to resonances

dominant contribution from $\Delta(1232 \text{ MeV})$

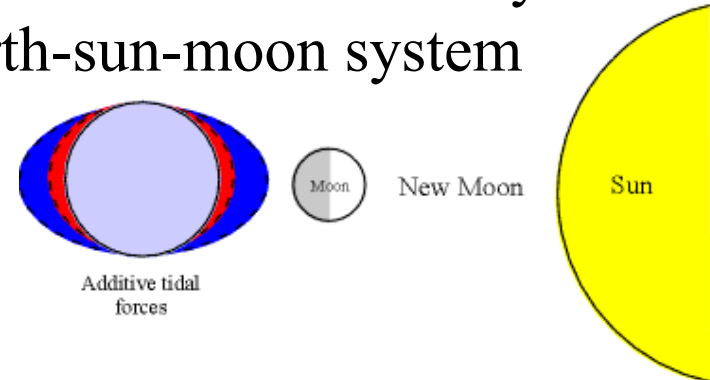


+ many shorter-range parts

chiral effective field theory (EFT)
Delta-less (Δ is treated as heavy):



tidal effects lead to 3-body forces
in earth-sun-moon system

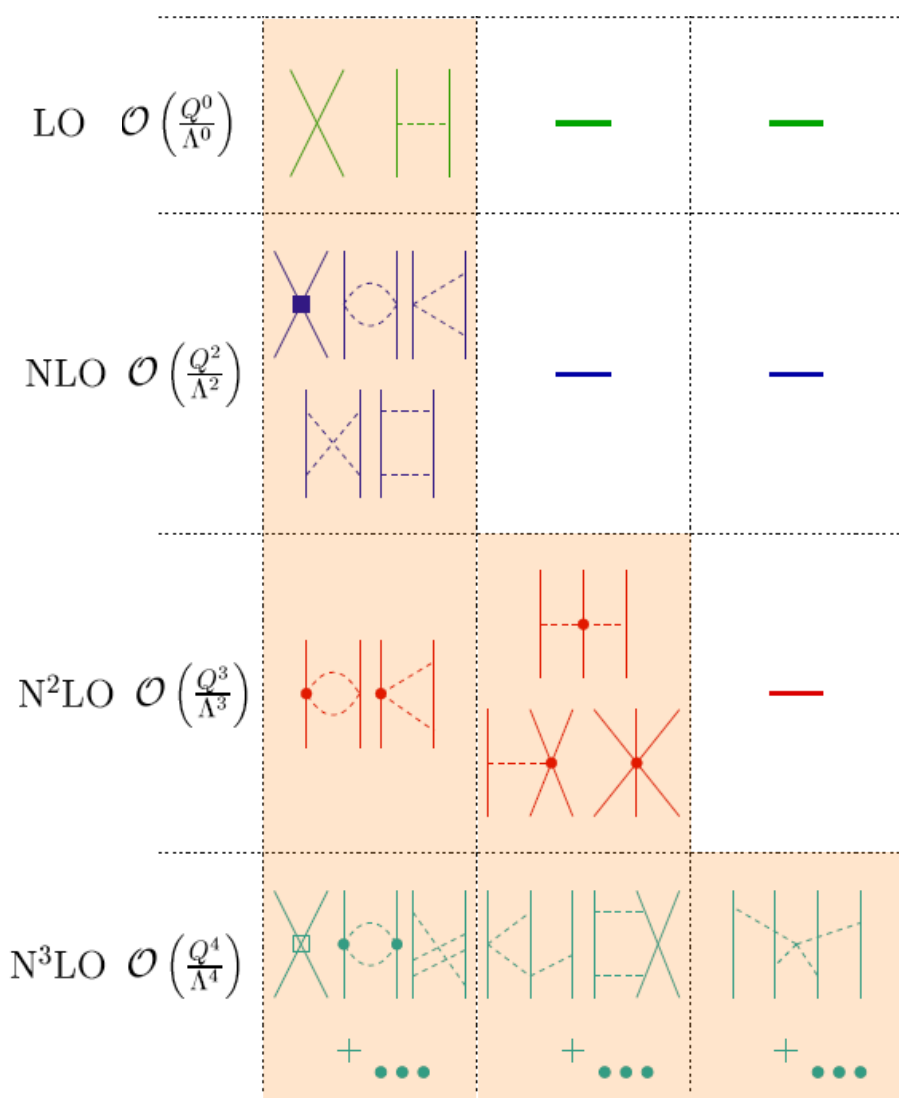


EFT provides a systematic and powerful approach for 3N forces

Chiral effective field theory for nuclear forces

Separation of scales: low momenta $\frac{1}{\lambda} = Q \ll \Lambda_{\text{breakdown}}$ scale ~ 500 MeV

NN 3N 4N



limited resolution at low energies,
can expand in powers $(Q/\Lambda_b)^n$

LO, $n=0$ - leading order,
NLO, $n=2$ - next-to-leading order,...

expansion parameter $\sim 1/3$

(compare to multipole expansion
for a charge distribution)

Chiral effective field theory for nuclear forces

Separation of scales: low momenta $\frac{1}{\lambda} = Q \ll \Lambda_{\text{breakdown}} \sim 500 \text{ MeV}$

NN 3N 4N

LO $\mathcal{O}\left(\frac{Q^0}{\Lambda^0}\right)$				include long-range pion physics
NLO $\mathcal{O}\left(\frac{Q^2}{\Lambda^2}\right)$				few short-range couplings, fit to experiment once
N ² LO $\mathcal{O}\left(\frac{Q^3}{\Lambda^3}\right)$				consistent electroweak interactions and matching to lattice QCD
N ³ LO $\mathcal{O}\left(\frac{Q^4}{\Lambda^4}\right)$				

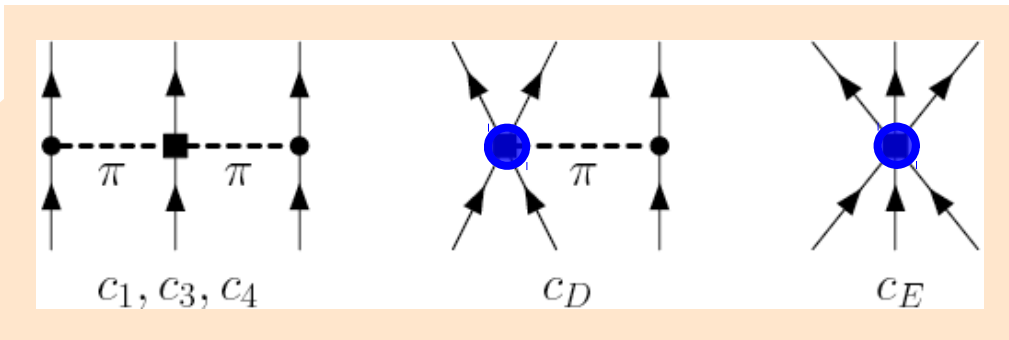
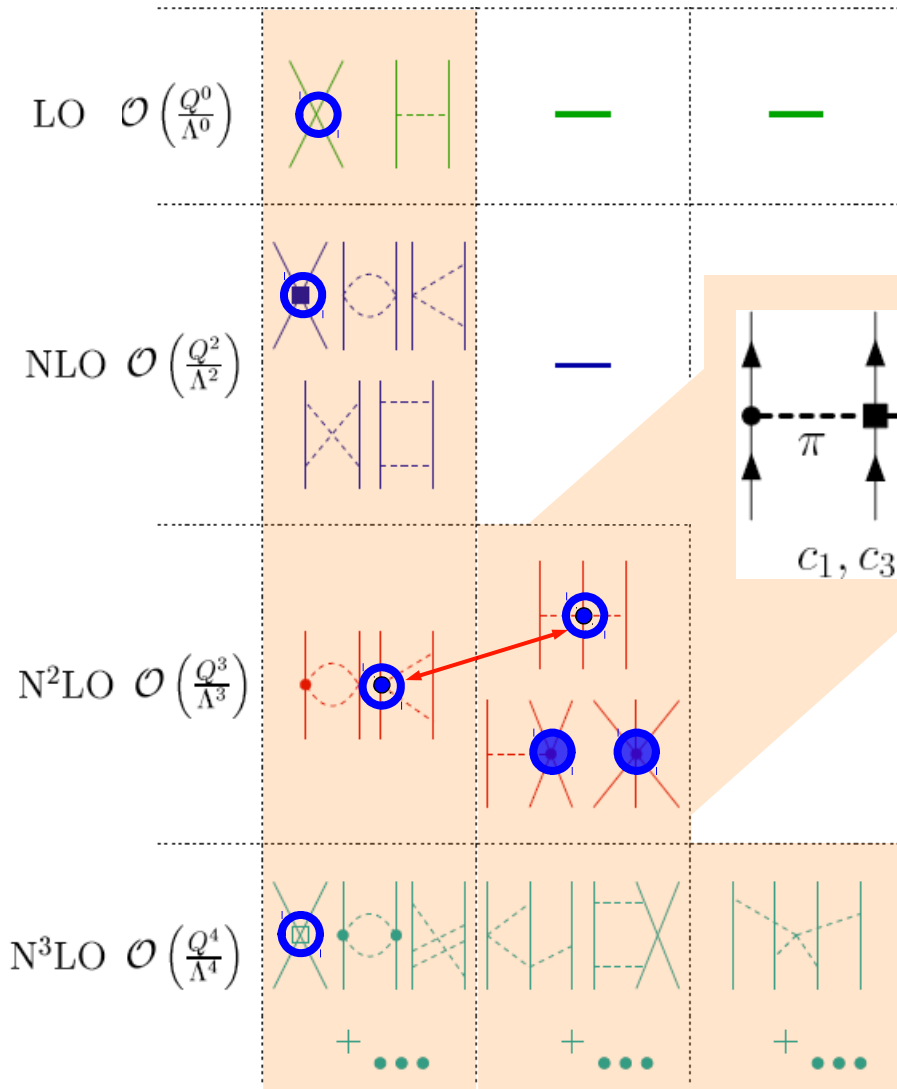
Chiral effective field theory and many-body forces

Separation of scales: low momenta $\frac{1}{\lambda} = Q \ll \Lambda$ breakdown scale ~ 500 MeV

NN 3N 4N

consistent NN-3N-4N interactions

3N,4N: **2 new couplings to N3LO**



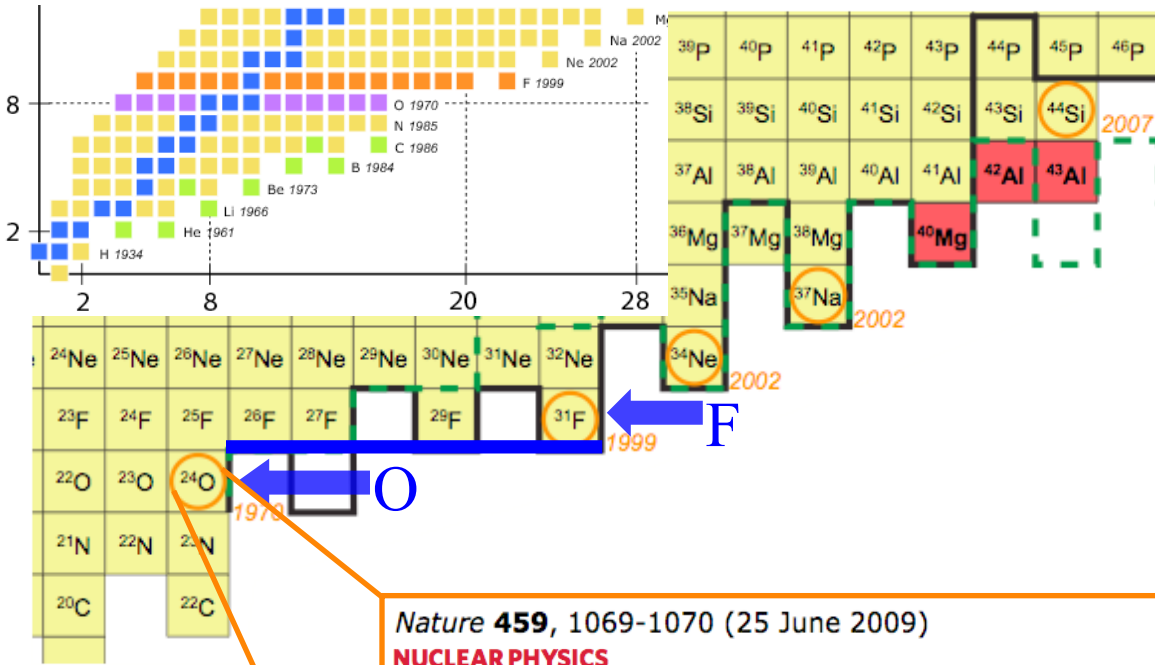
c_i from πN and NN [Meissner et al. \(2007\)](#)

$$c_1 = -0.9_{-0.5}^{+0.2}, \quad c_3 = -4.7_{-1.0}^{+1.2}, \quad c_4 = 3.5_{-0.2}^{+0.5}$$

single- Δ : $c_1=0, c_3=-c_4/2=-3$ GeV $^{-1}$

c_D, c_E fit to $^3\text{H}, ^4\text{He}$ properties only

The oxygen anomaly



Nature **459**, 1069-1070 (25 June 2009)

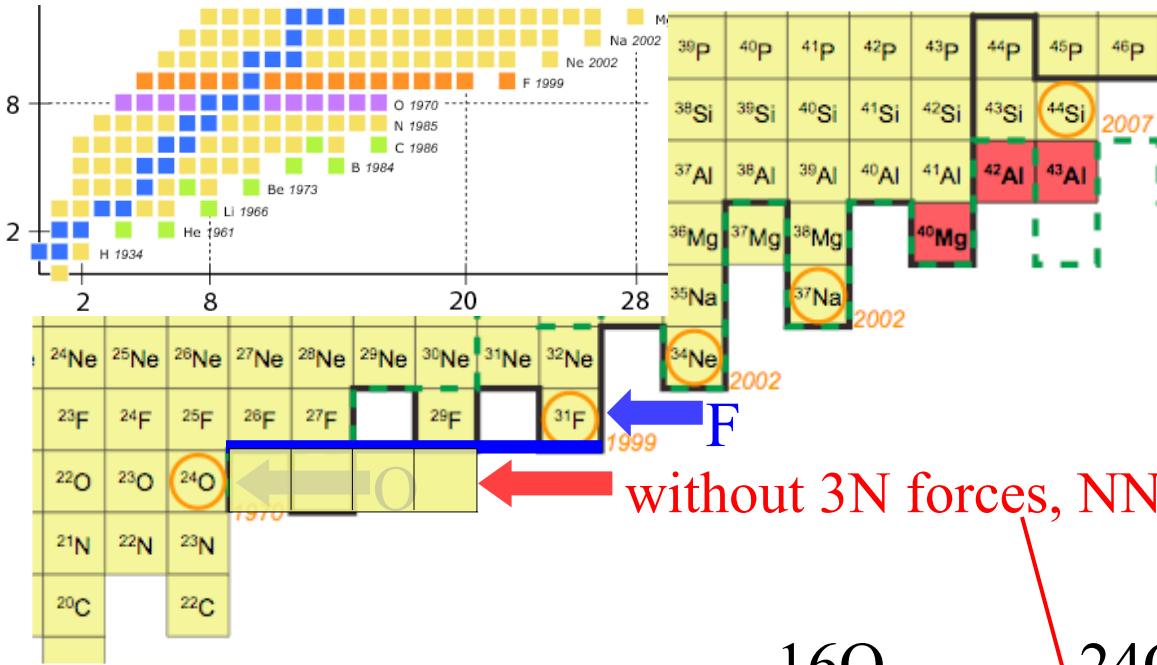
NUCLEAR PHYSICS

Unexpected doubly magic nucleus

Robert V. F. Janssens

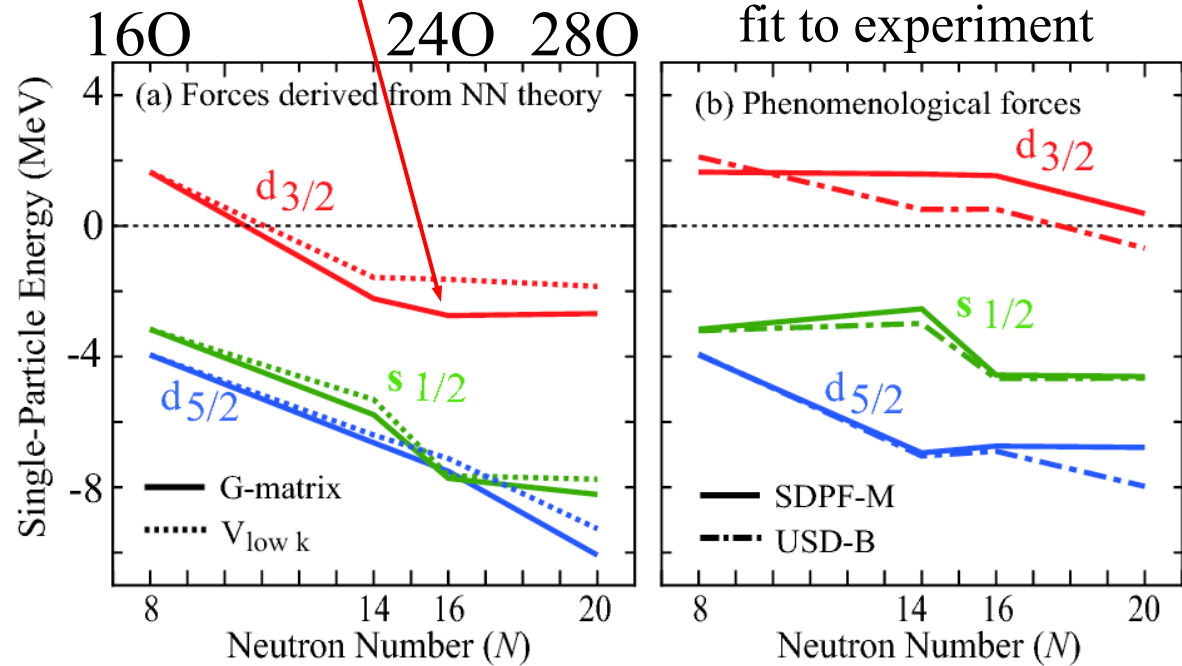
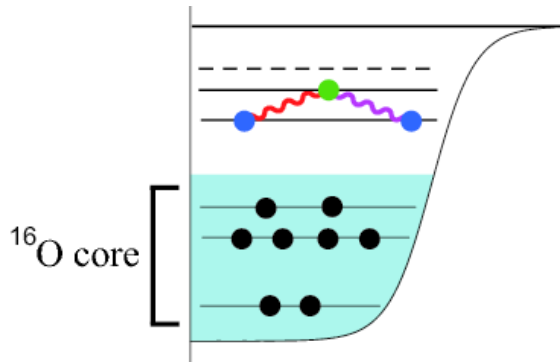
Nuclei with a 'magic' number of both protons and neutrons, dubbed doubly magic, are particularly stable. The oxygen isotope ^{24}O has been found to be one such nucleus — yet it lies just at the limit of stability.

The oxygen anomaly - not reproduced without 3N forces



without 3N forces, NN interactions too attractive

many-body theory based on two-nucleon forces:
drip-line incorrect at 28O



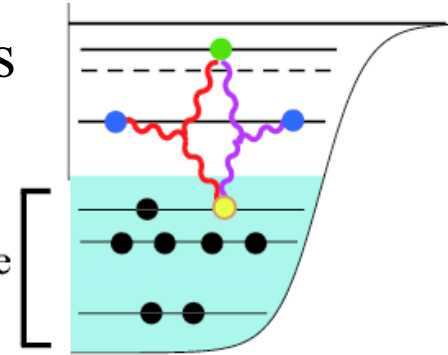
The shell model - impact of 3N forces

include 'normal-ordered' 2-body part of 3N forces (enhanced by core A)

leads to repulsive interactions between valence neutrons

contributions from residual three valence-nucleon interactions suppressed by $E_{ex}/E_F \sim N_{valence}/N_{core}$

Friman, AS (2011)



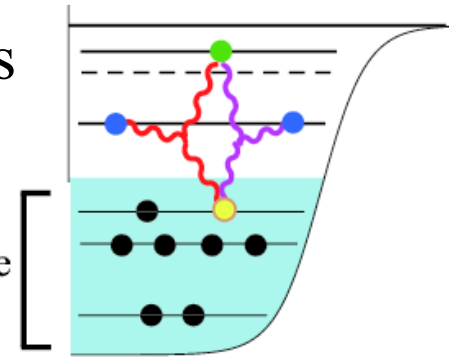
Oxygen isotopes - impact of 3N forces

include ‘normal-ordered’ 2-body part of 3N forces (enhanced by core A)

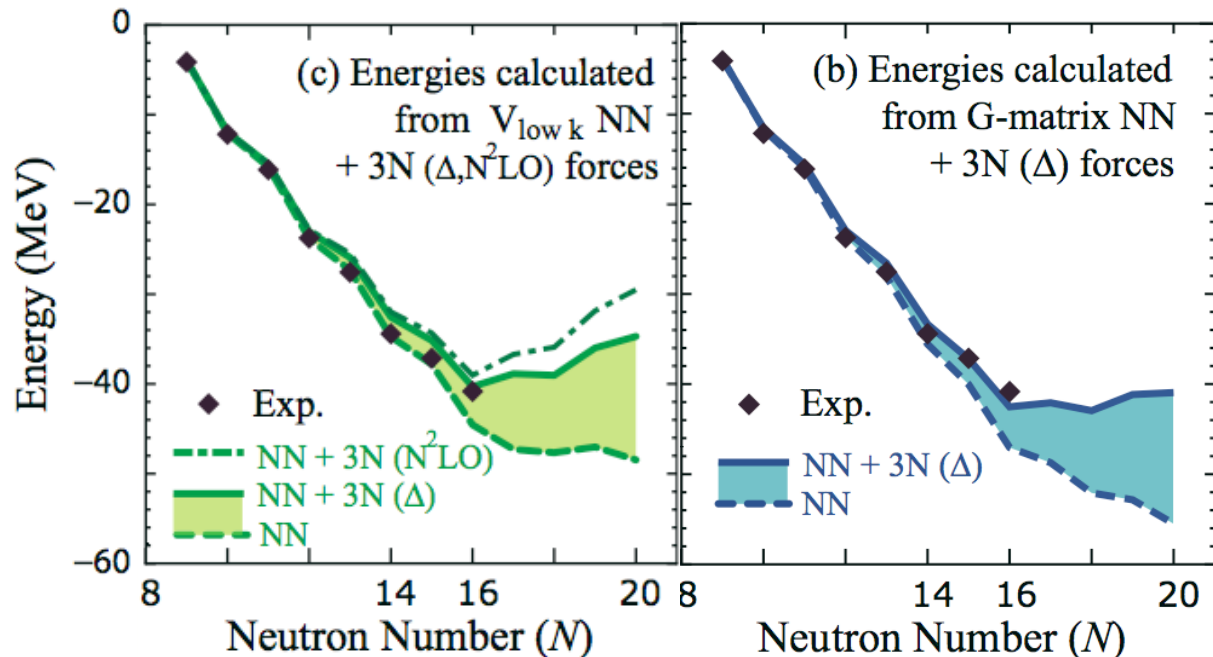
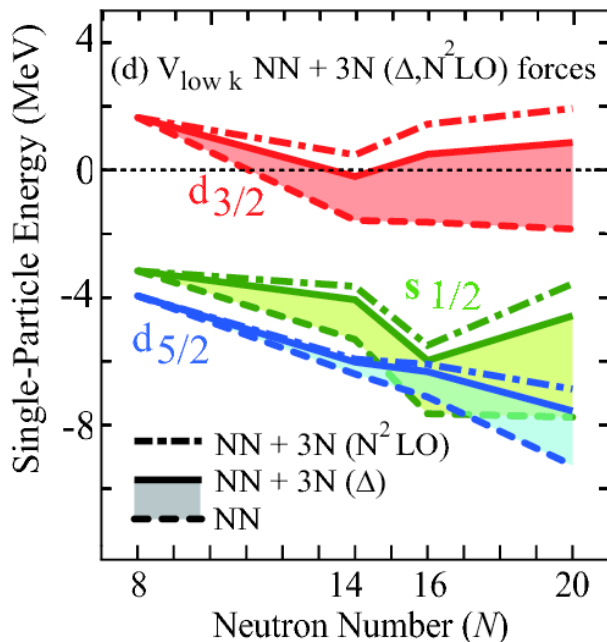
leads to repulsive interactions between valence neutrons

contributions from residual three valence-nucleon interactions suppressed by $E_{ex}/E_F \sim N_{valence}/N_{core}$

Friman, AS (2011)



$d_{3/2}$ orbital remains unbound from ^{16}O to ^{28}O



microscopic explanation of the oxygen anomaly Otsuka et al. (2010)

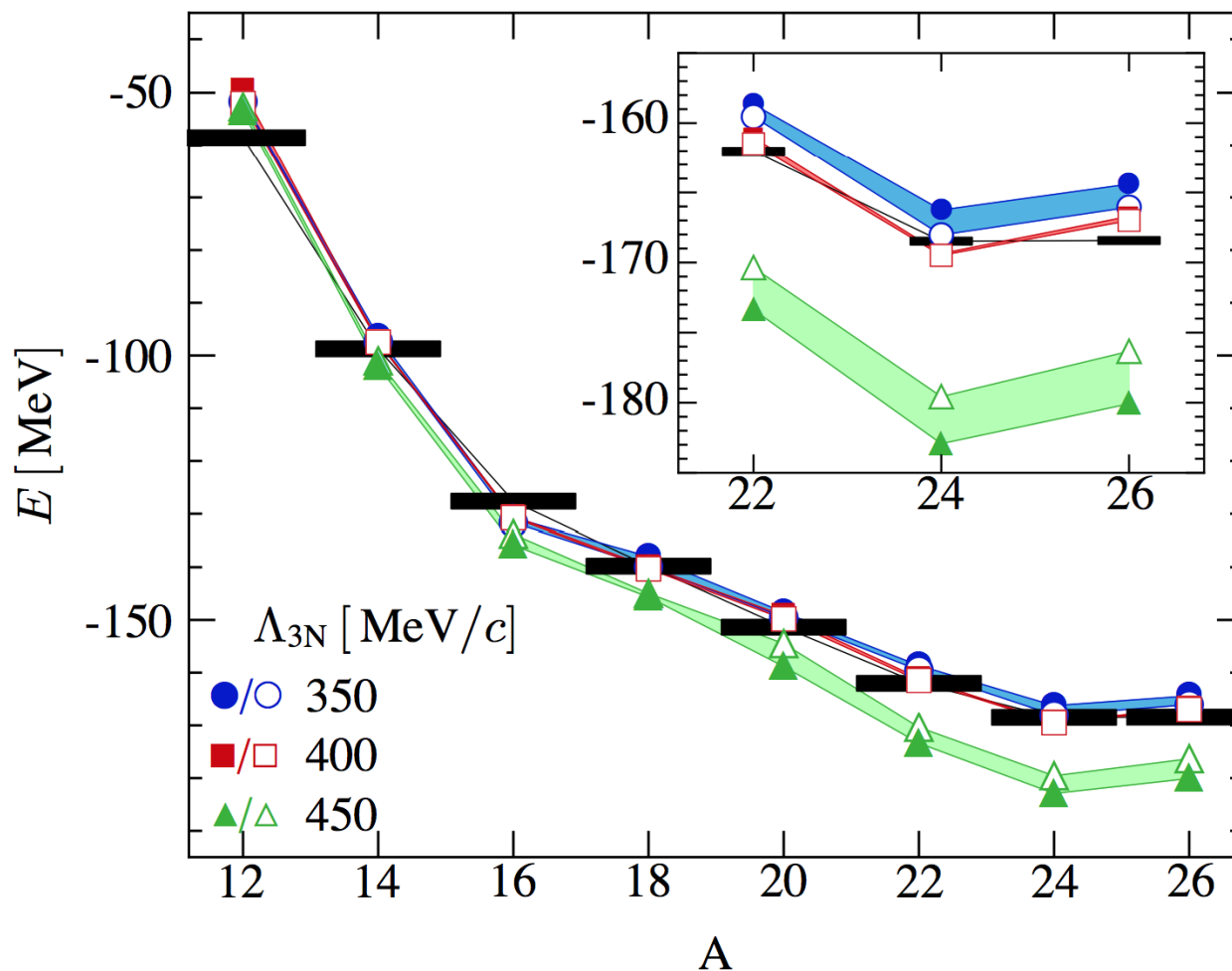
New ab-initio methods extend reach

impact of 3N forces confirmed in large-space calculations:

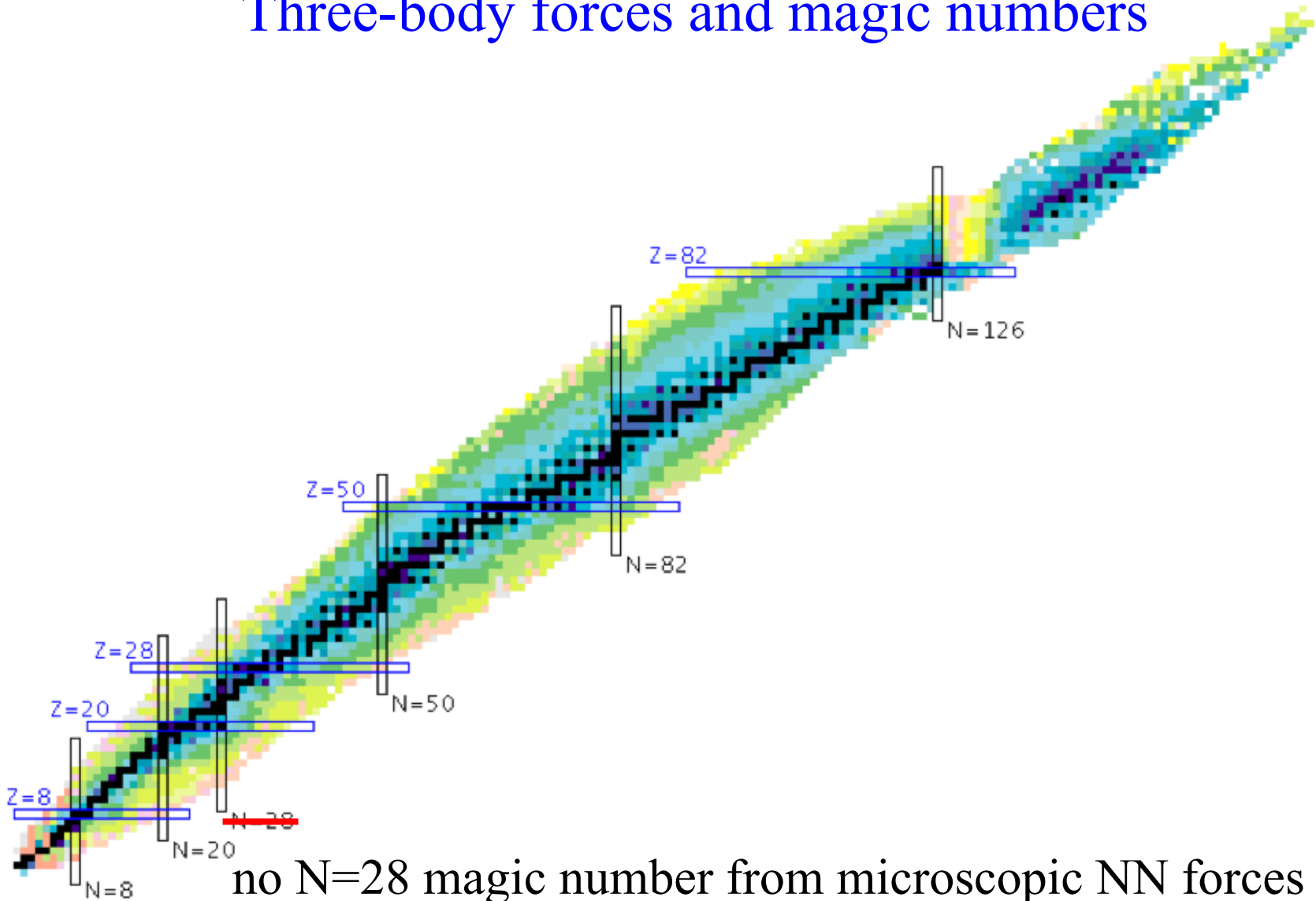
Coupled Cluster theory with phenomenological 3N forces [Hagen et al. \(2012\)](#)

In-Medium Similarity RG based on chiral NN+3N [Hergert et al. \(2013\)](#)

Green's function methods based on chiral NN+3N [Cipollone et al. \(2013\)](#)



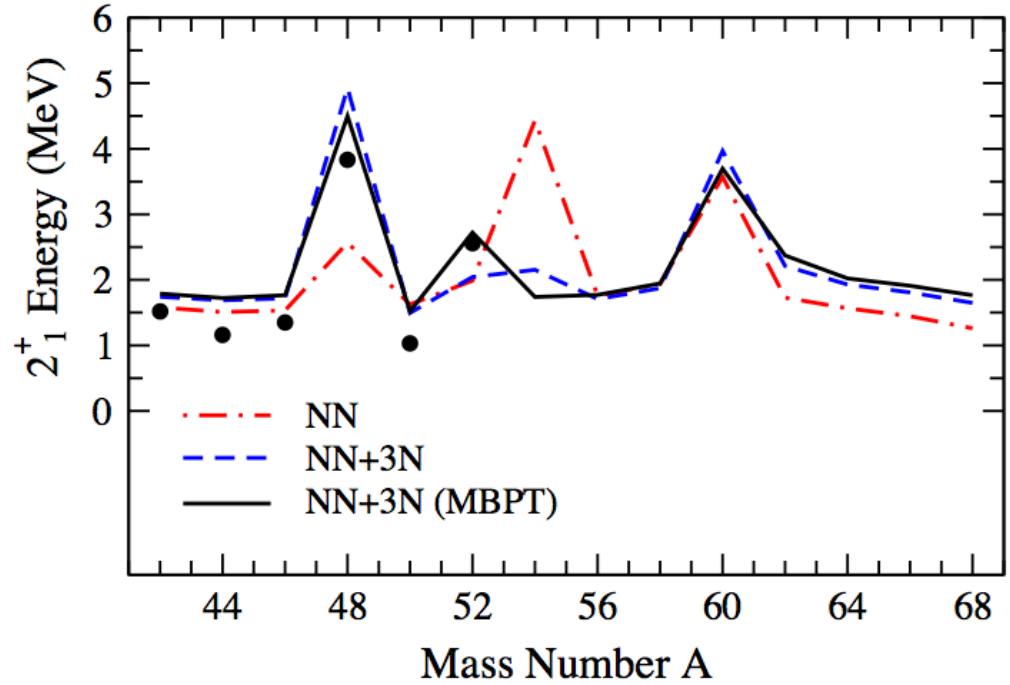
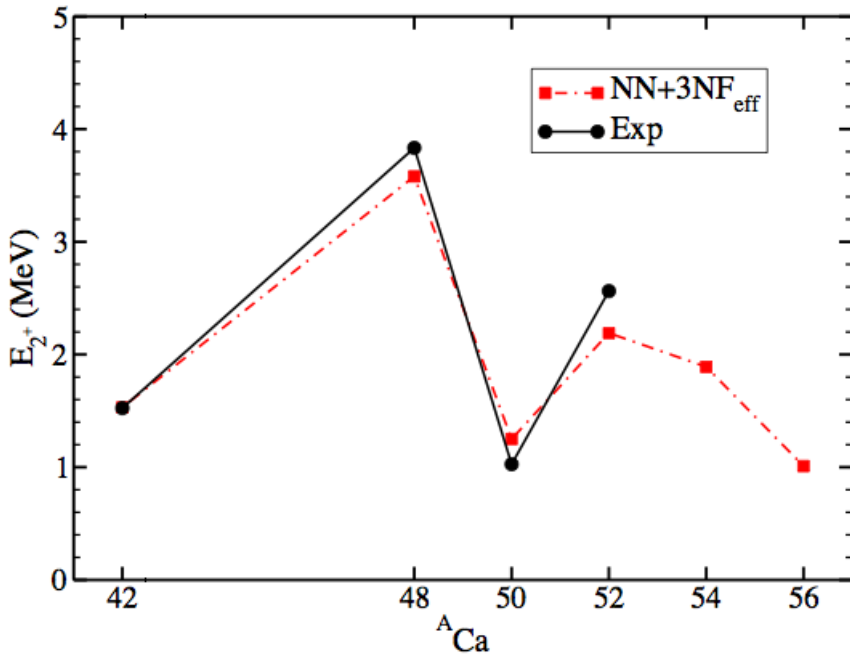
Three-body forces and magic numbers



no $N=28$ magic number from microscopic NN forces

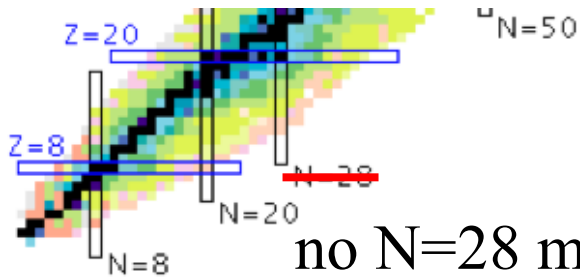
Zuker, Poves,...

Three-body forces and magic numbers



Hagen et al. (2012)

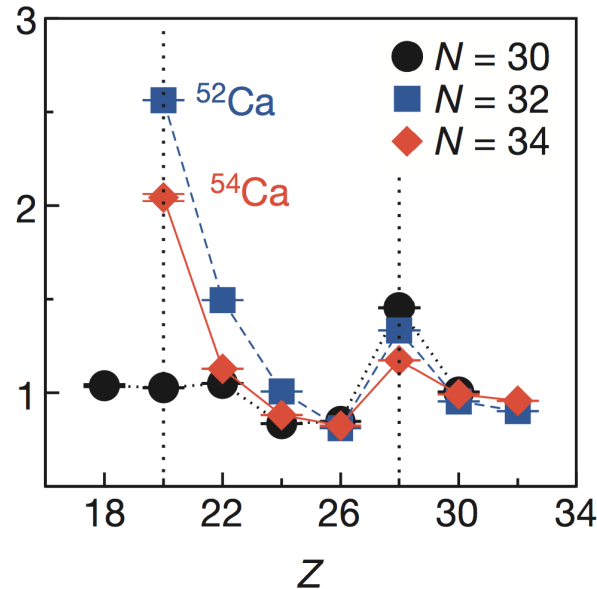
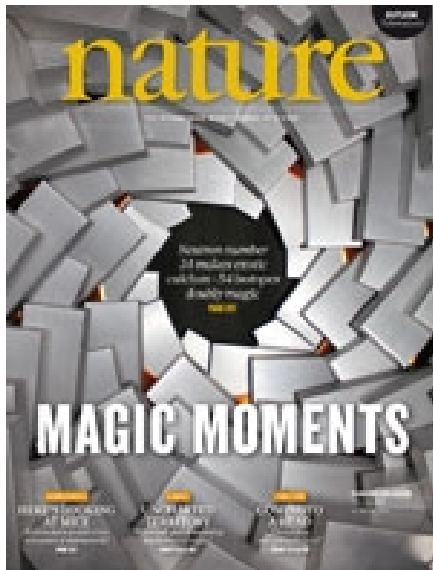
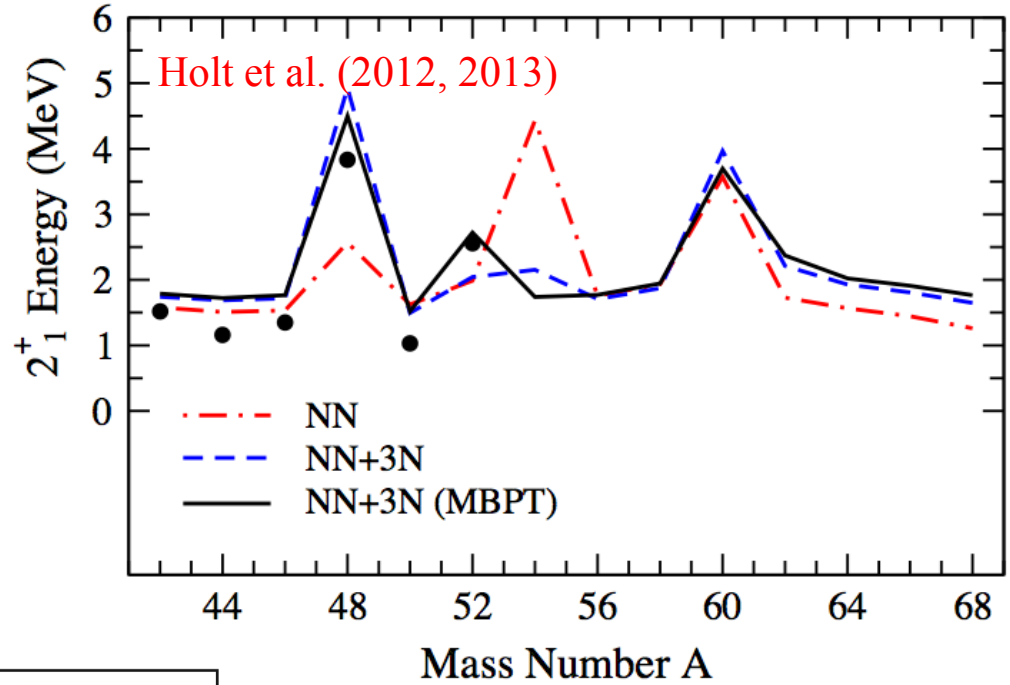
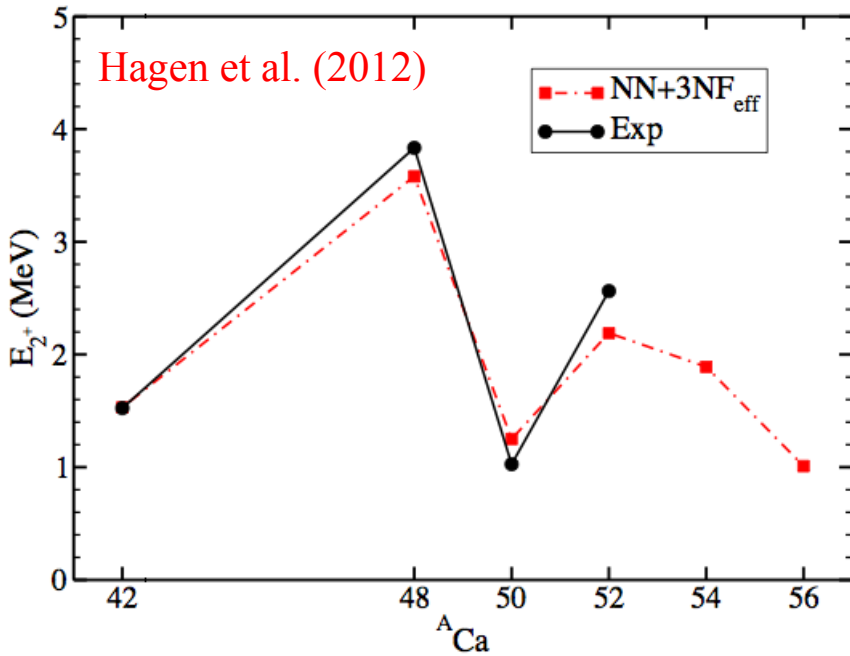
Holt et al. (2012, 2013)



no $N=28$ magic number from microscopic NN forces

Zuker, Poves, ...

Three-body forces and magic numbers



2^+ energy measured at RIBF suggests magic number $N=34$
 Steppenbeck et al. (2013)

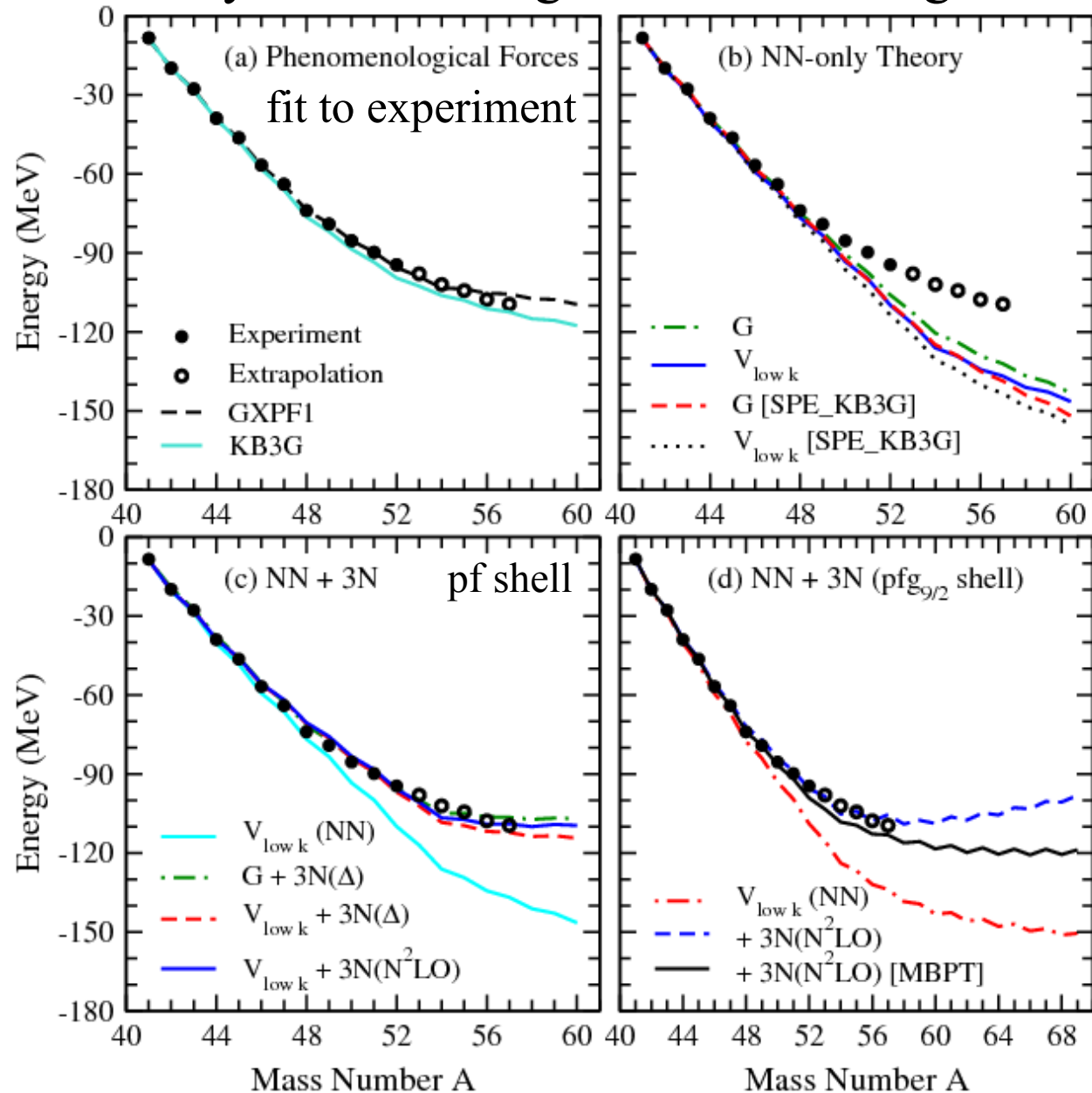
Evolution to neutron-rich calcium isotopes

repulsive 3N contributions also key for calcium ground-state energies

Holt, Otsuka, AS, Suzuki (2012)

mass measured to ^{52}Ca
shown to exist to ^{58}Ca

gs energy flat with N,
continuum important
for dripline location!



Evolution to neutron-rich calcium isotopes

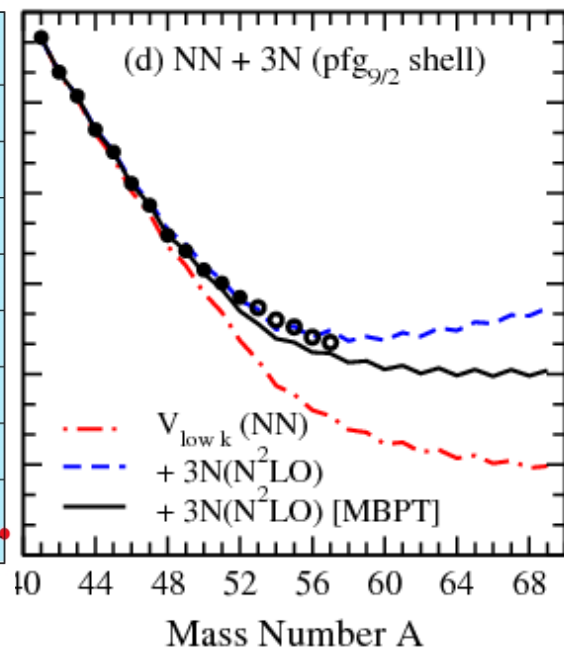
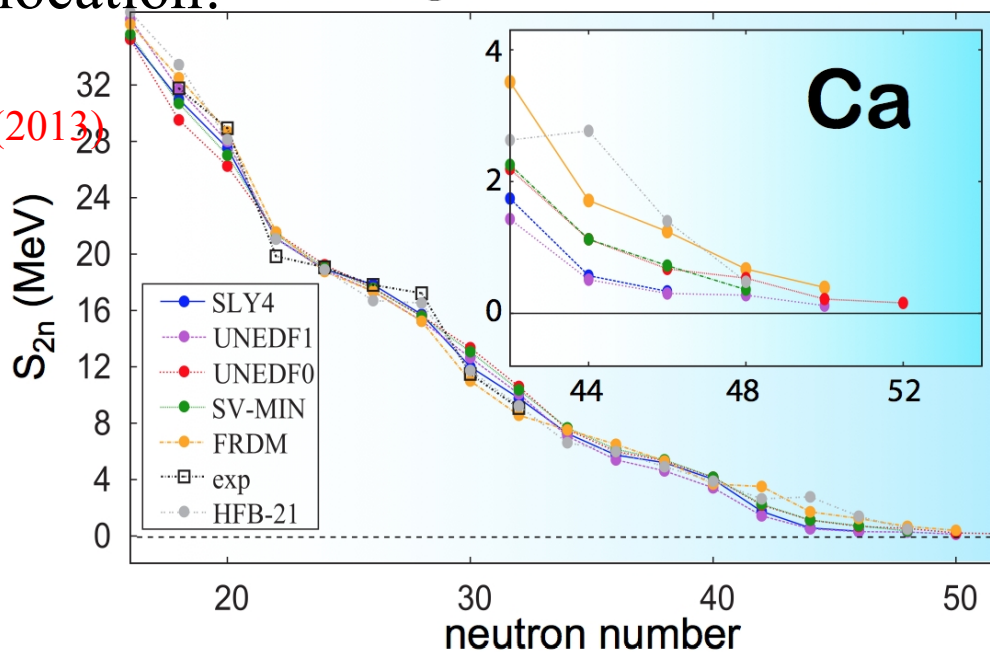
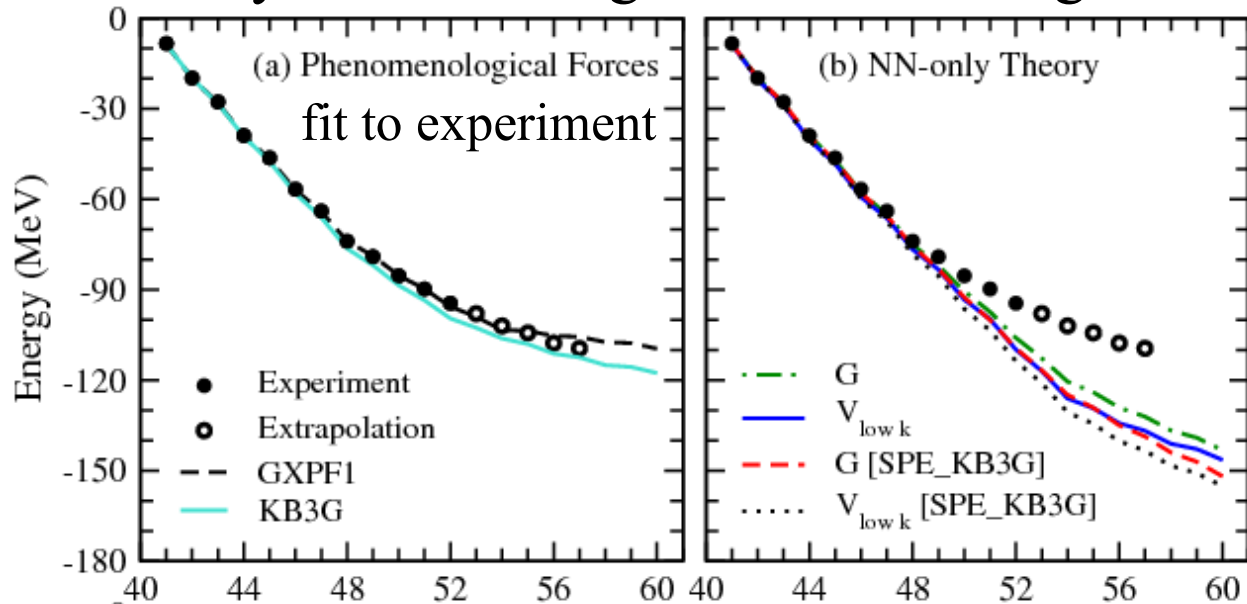
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see Forssen et al. (2013)

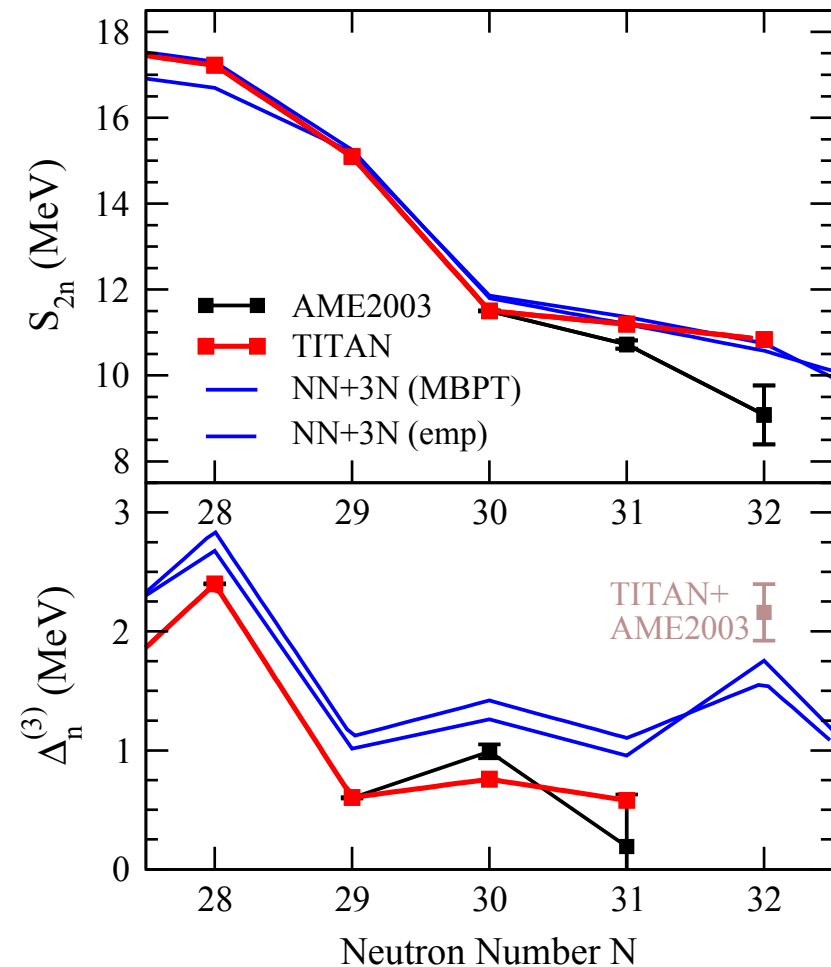
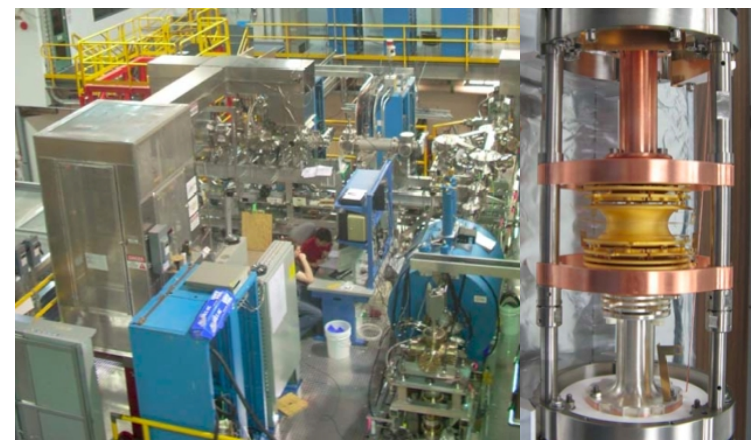


new $^{51,52}\text{Ca}$ TITAN measurements

^{52}Ca is 1.75 MeV more bound compared to atomic mass evaluation

Gallant et al. (2012)

behavior of $2n$ separation energy S_{2n} agrees with NN+3N predictions



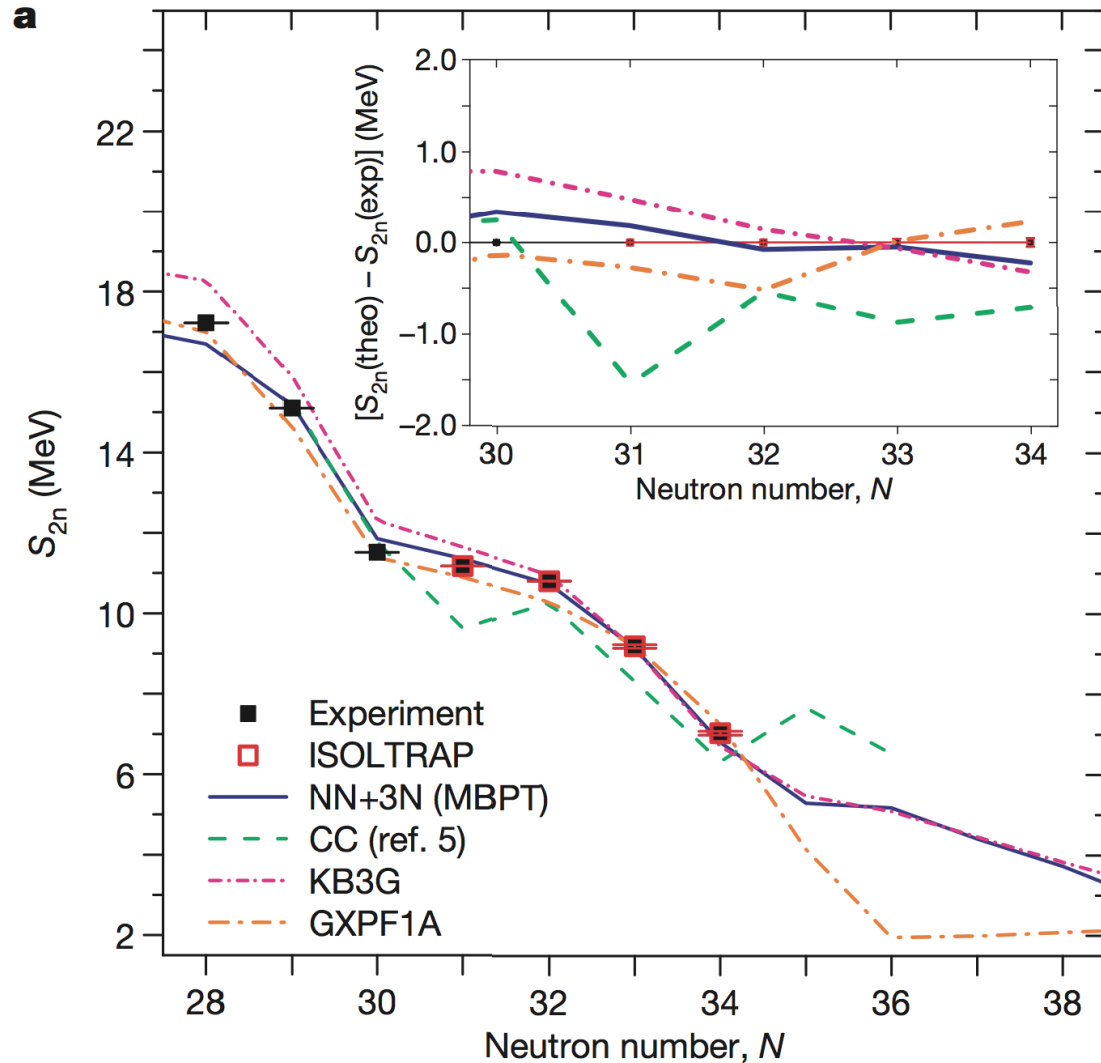
Masses of exotic calcium isotopes pin down nuclear forces

F. Wienholtz¹, D. Beck², K. Blaum³, Ch. Borgmann³, M. Breitenfeldt⁴, R. B. Cakirli^{3,5}, S. George¹, F. Herfurth², J. D. Holt^{6,7}, M. Kowalska⁸, S. Kreim^{3,8}, D. Lunney⁹, V. Manea⁹, J. Menéndez^{6,7}, D. Neidherr², M. Rosenbusch¹, L. Schweikhard¹, A. Schwenk^{7,6}, J. Simonis^{6,7}, J. Stanja¹⁰, R. N. Wolf¹ & K. Zuber¹⁰

53,54Ca masses measured at ISOLTRAP using new MR-TOF mass spectrometer

establish prominent N=32 shell closure in calcium

excellent agreement with theoretical predictions



Masses of exotic calcium isotopes pin down nuclear forces

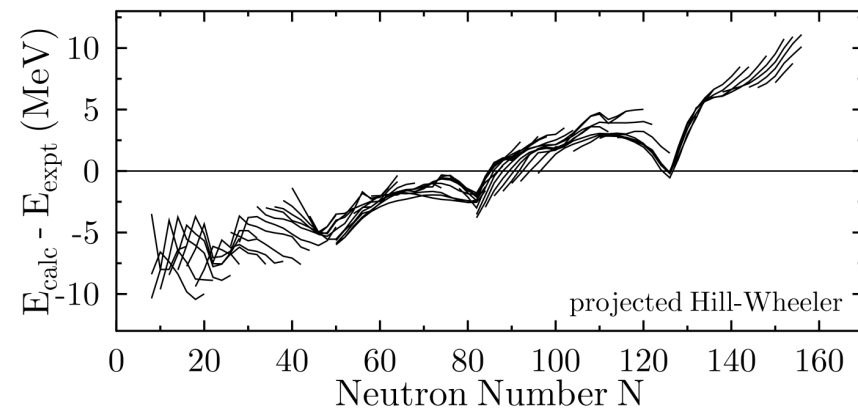
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overall good agreement with density functional predictions

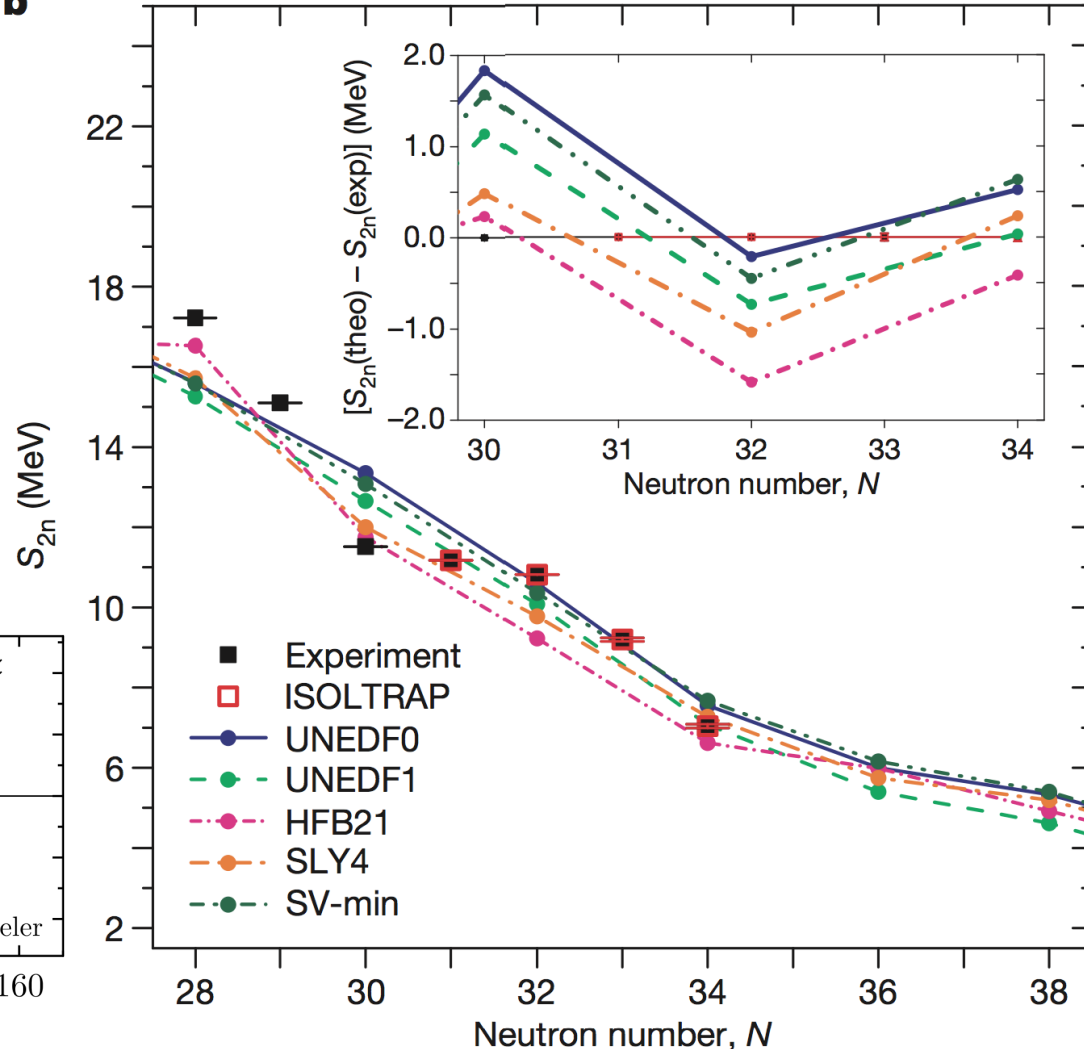
challenge to reproduce shell closures

cf. N=50, 82, 126 “arches”

Bender et al. (2005)

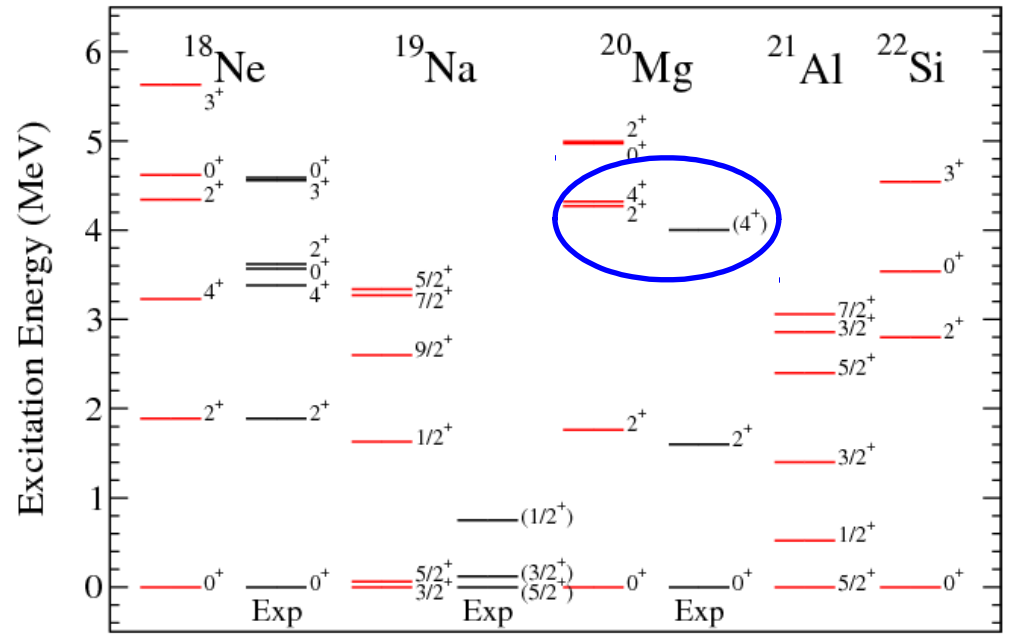
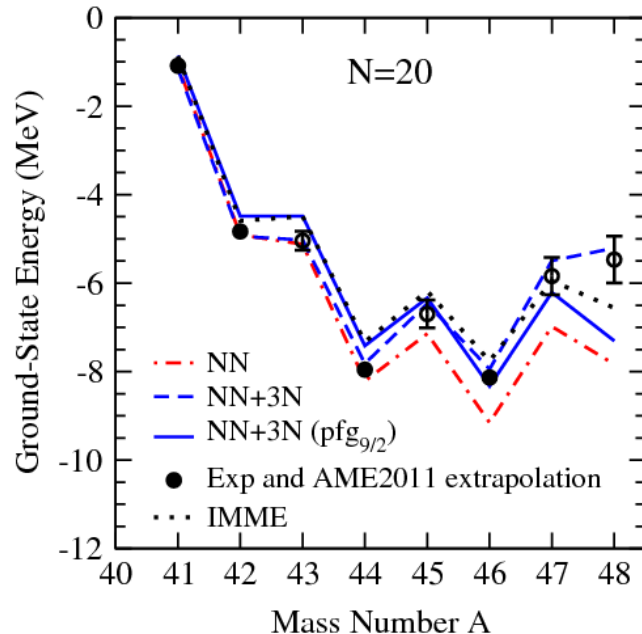
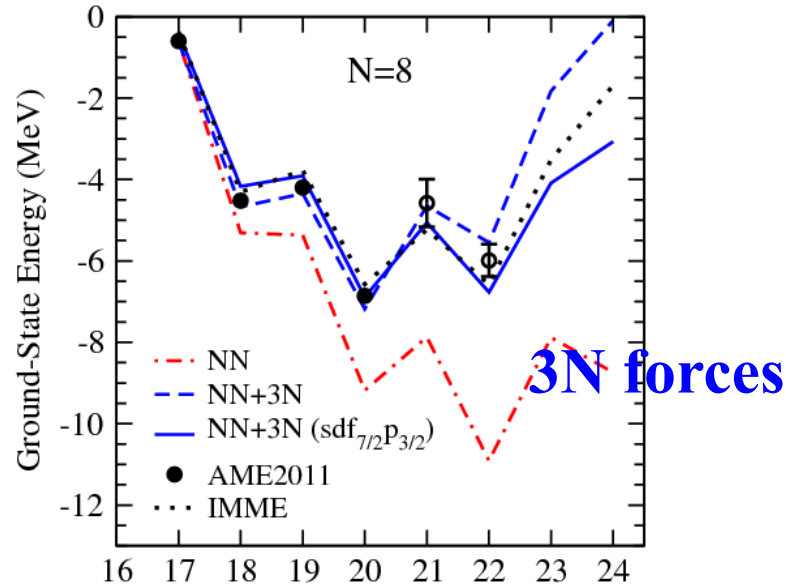


b



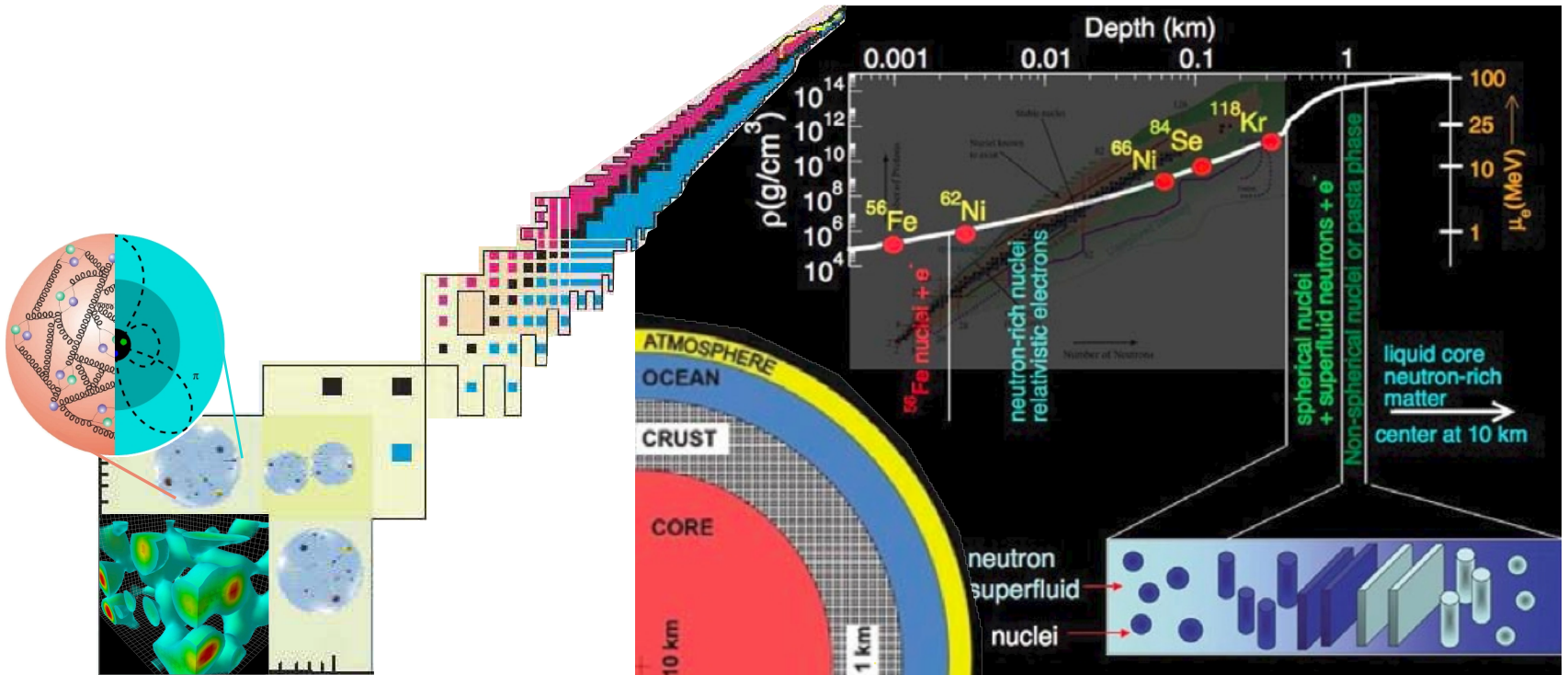
3N forces and proton-rich nuclei Holt, Menendez, AS (2013)

first results with 3N forces for ground and excited states of N=8, 20



prediction for ^{20}Mg agrees with new state observed at GSI Mukha, private comm.

Neutron matter and neutron stars

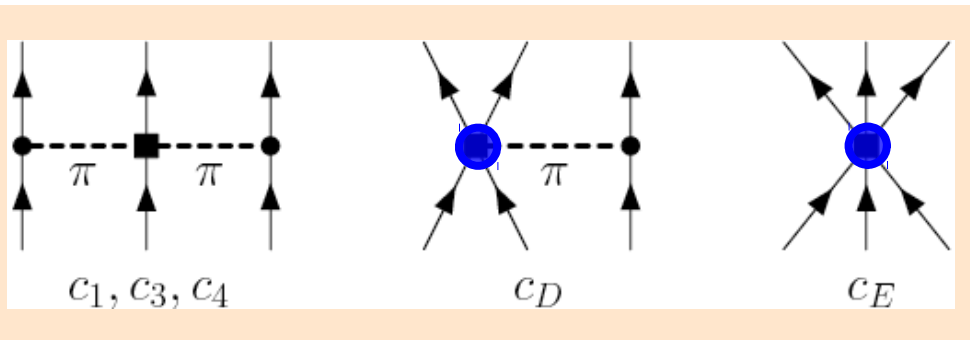
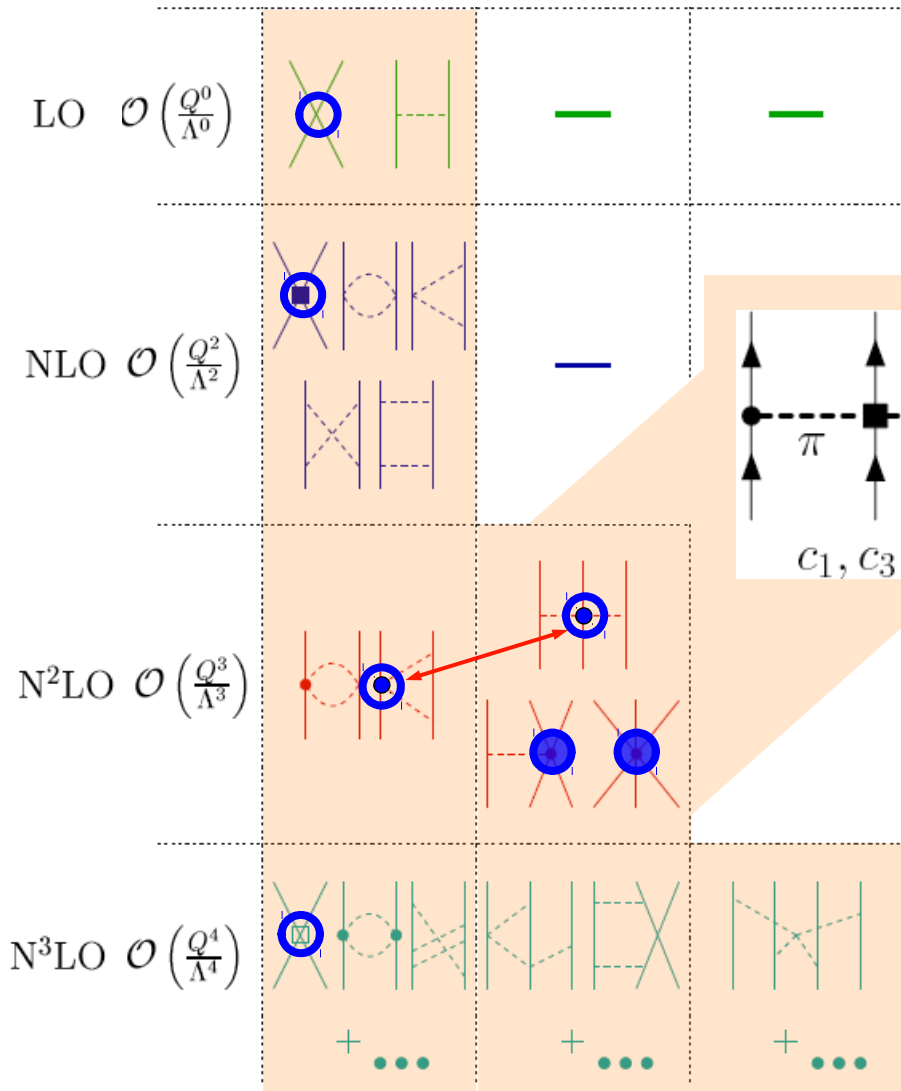


Chiral effective field theory for nuclear forces

Separation of scales: low momenta $\frac{1}{\lambda} = Q \ll \text{breakdown scale} \sim 500 \text{ MeV}$

NN 3N 4N

cD, cE don't contribute for **neutrons** because of Pauli principle and pion coupling to spin, also for c4
 Hebeler, AS (2010)



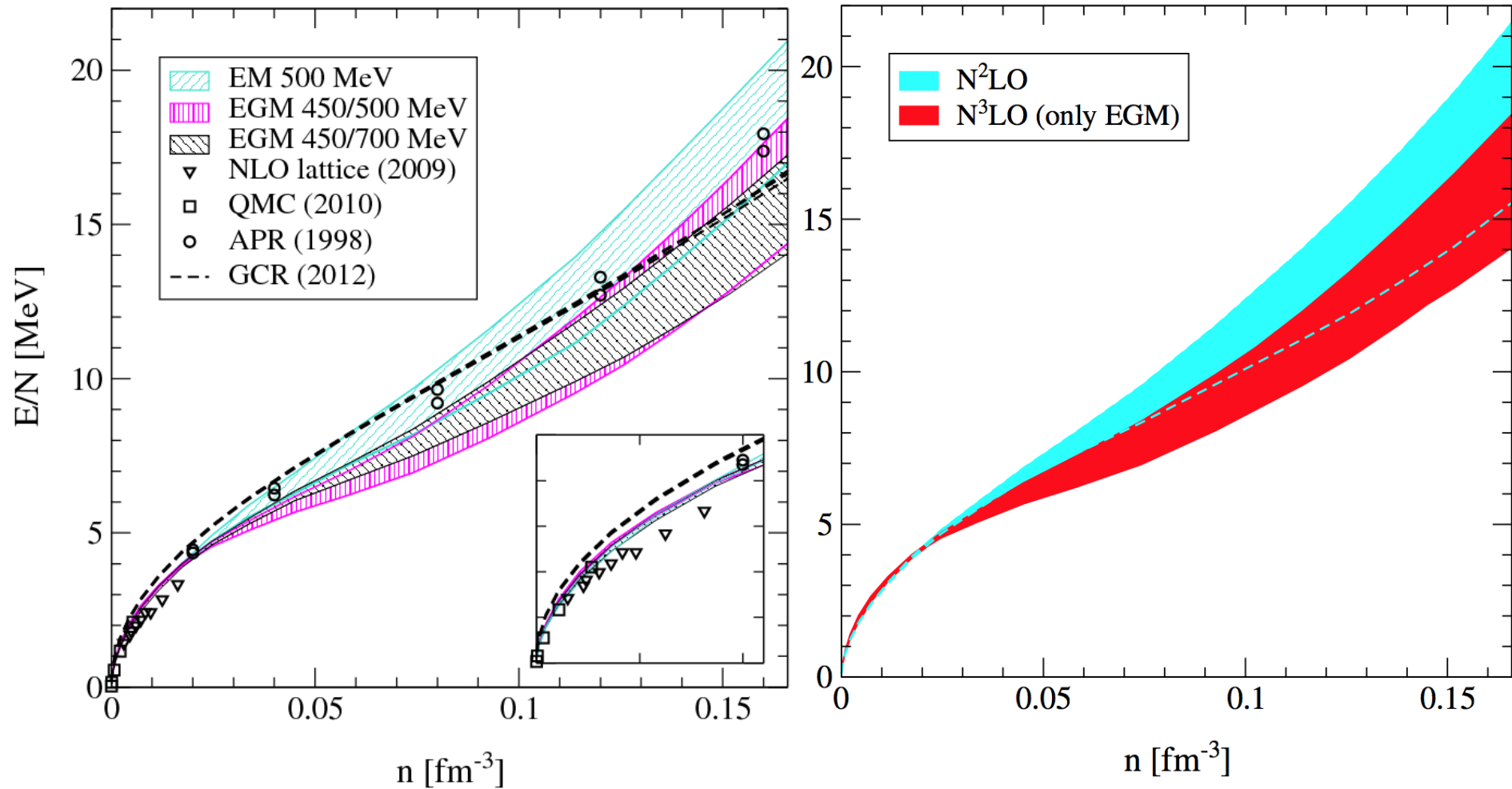
all 3- and 4-neutron forces are predicted to N3LO!

study 3N and 4N in neutron matter
 Tews, Krüger, Hebeler, AS (2013)

Complete N3LO calculation of neutron matter

first complete N3LO result [Tews, Krüger, Hebeler, AS \(2013\)](#)

includes uncertainties from NN, 3N (dominates), 4N

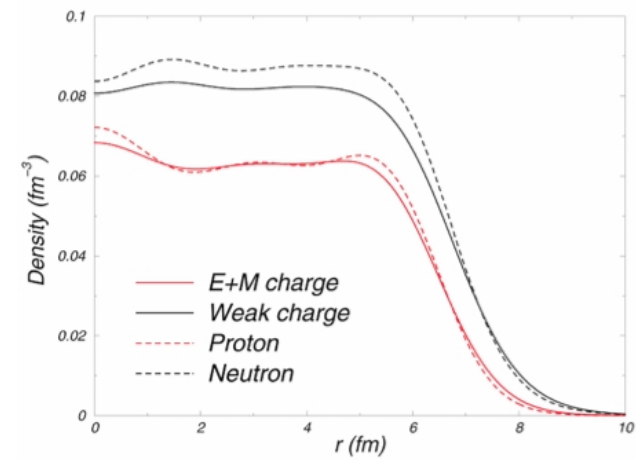


Neutron skin of ^{208}Pb

probes neutron matter energy/pressure,
neutron matter band predicts

neutron skin of ^{208}Pb : 0.17 ± 0.03 fm ($\pm 18\%$!)

Hebeler et al. (2010)

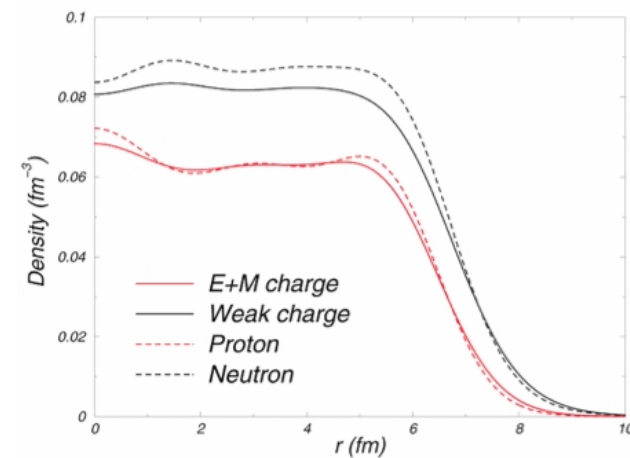


Neutron skin of ^{208}Pb

probes neutron matter energy/pressure,
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neutron skin of ^{208}Pb : 0.17 ± 0.03 fm ($\pm 18\%$!)

Hebeler et al. (2010)



in excellent agreement with extraction from complete E1 response
 $0.156 + 0.025 - 0.021$ fm

PRL 107, 062502 (2011)

PHYSICAL REVIEW LETTERS

week ending
5 AUGUST 2011

Complete Electric Dipole Response and the Neutron Skin in ^{208}Pb

A benchmark experiment on ^{208}Pb shows that polarized proton inelastic scattering at very forward angles including 0° is a powerful tool for high-resolution studies of electric dipole ($E1$) and spin magnetic dipole ($M1$) modes in nuclei over a broad excitation energy range to test up-to-date nuclear models. The extracted $E1$ polarizability leads to a neutron skin thickness $r_{\text{skin}} = 0.156^{+0.025}_{-0.021}$ fm in ^{208}Pb derived within

PREX: neutron skin from parity-violating electron-scattering at JLAB

electron exchanges Z-b

PRL 108, 112502 (2012)

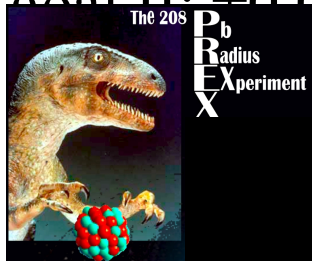
PHYSICAL REVIEW LETTERS

week ending
16 MARCH 2012

neutron skin: $+0.06$ fm

Measurement of the Neutron Radius of ^{208}Pb through Parity Violation in Electron Scattering

We report the first measurement of the parity-violating asymmetry A_{PV} in the elastic scattering of polarized electrons from ^{208}Pb . A_{PV} is sensitive to the radius of the neutron distribution (R_n). The result $A_{\text{PV}} = 0.656 \pm 0.060(\text{stat}) \pm 0.014(\text{syst})$ ppm corresponds to a difference between the radii of the neutron and proton distributions $R_n - R_p = 0.33^{+0.16}_{-0.18}$ fm and provides the first electroweak observation of the neutron skin which is expected in a heavy, neutron-rich nucleus.



Symmetry energy and pressure of neutron matter

neutron matter band predicts
symmetry energy S_v and
its density derivative L

comparison to experimental
and observational constraints

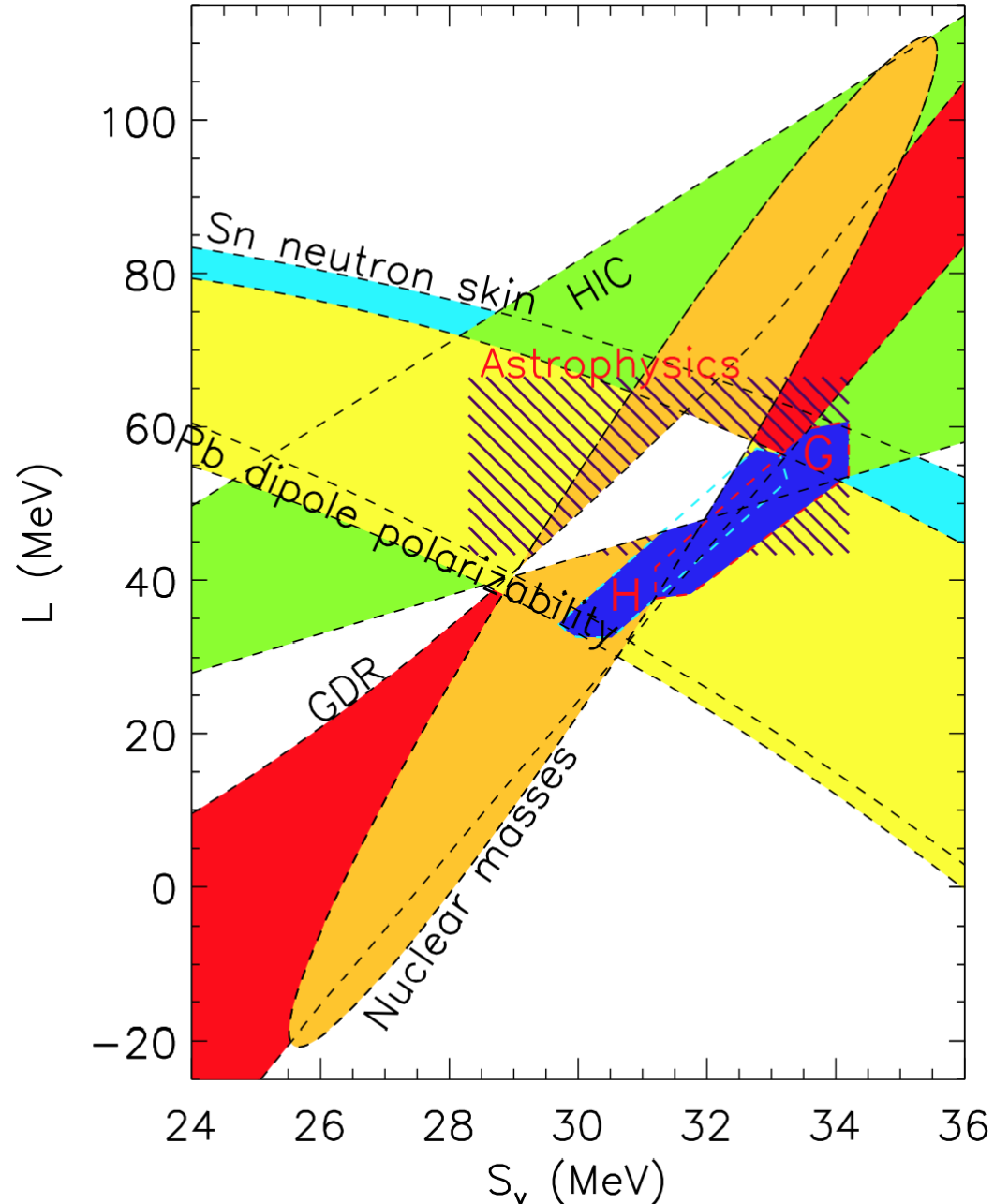
Lattimer, Lim (2013)

neutron matter constraints

H: Hebeler et al. (2010, 2013)

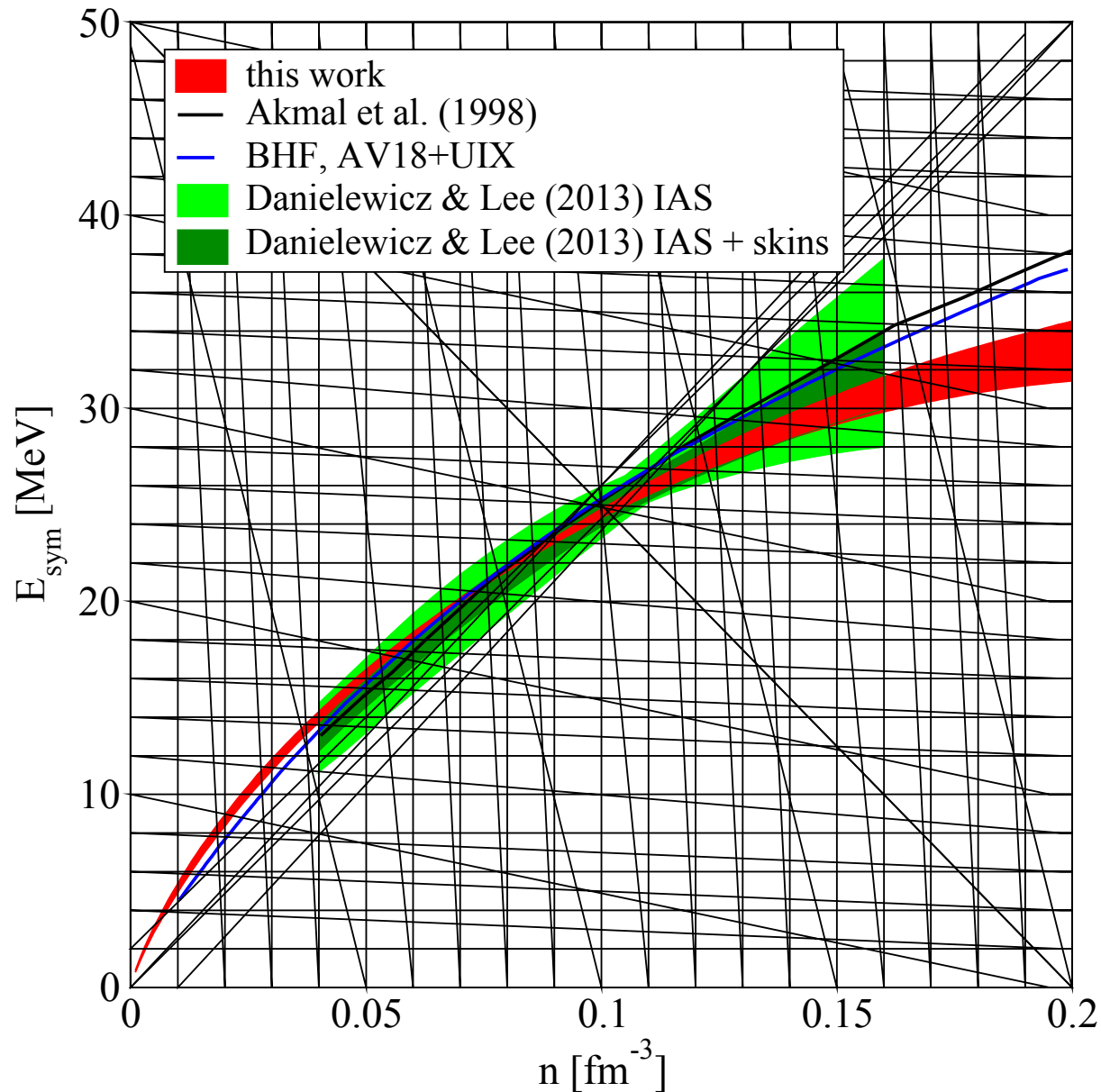
G: Gandolfi et al. (2011)

microscopic calculations
provide tight constraints!



Ab-initio calculations of asymmetric matter Drischler, Soma, AS (2013)

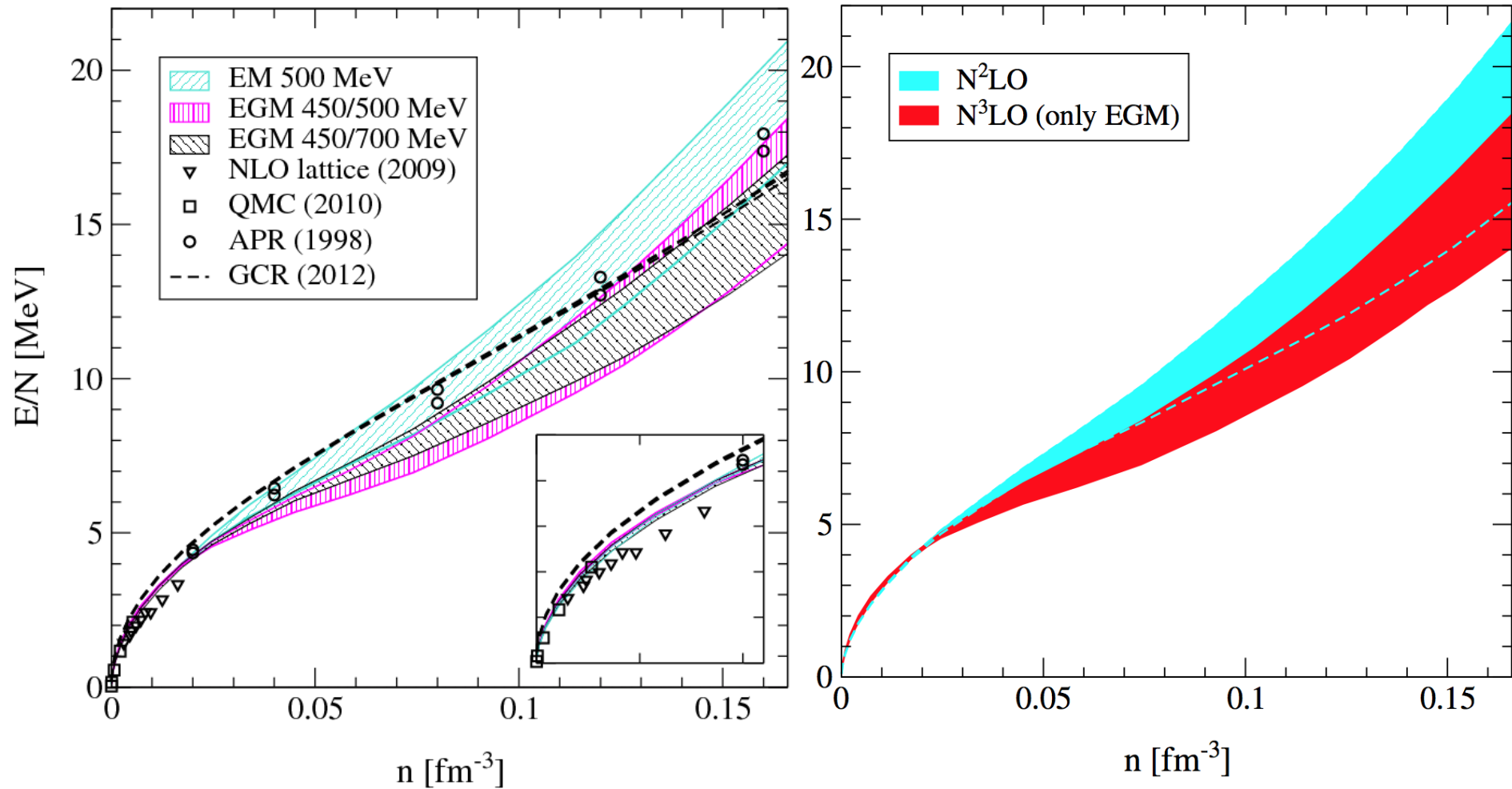
Esym comparison with extraction from isobaric analogue states (IAS)



Complete N3LO calculation of neutron matter

first complete N3LO result [Tews, Krüger, Hebeler, AS \(2013\)](#)

includes uncertainties from NN, 3N (dominates), 4N



Discovery of the heaviest neutron star

A two-solar-mass neutron star measured using Shapiro delay

P. B. Demorest¹, T. Pennucci², S. M. Ransom¹, M. S. E. Roberts³ & J. W. T. Hessels^{4,5}

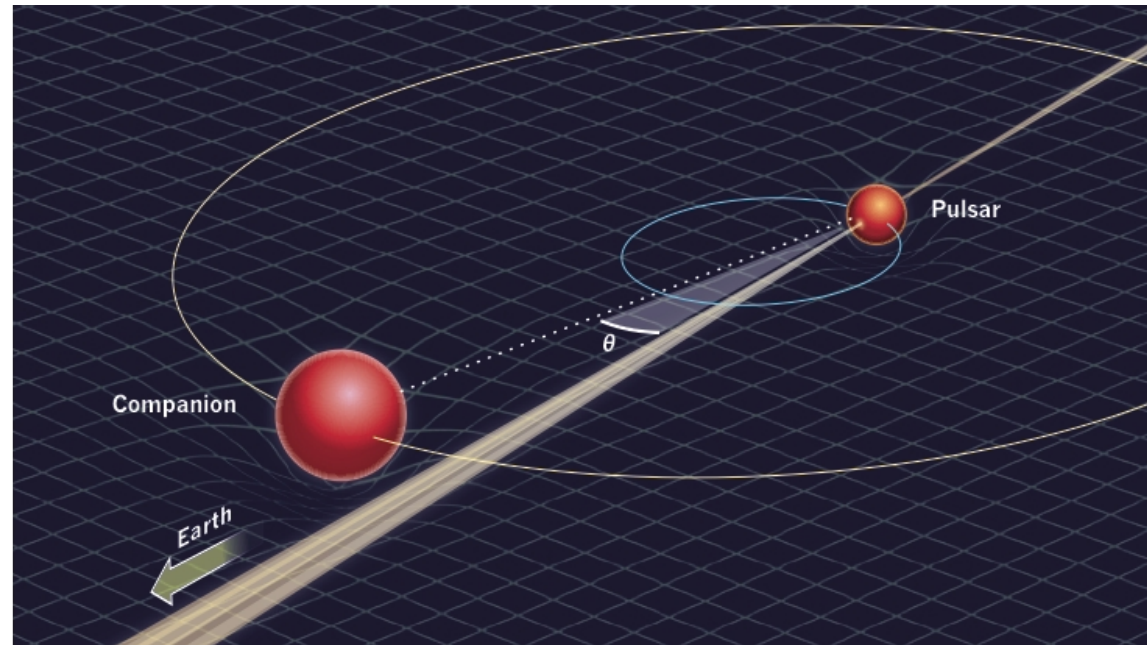
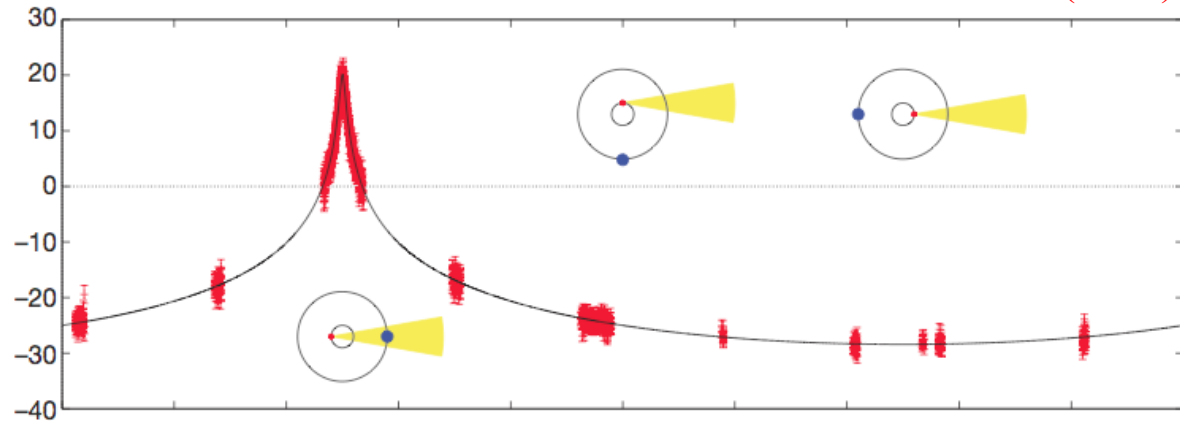
Nature (2010)

direct measurement of
neutron star mass from
increase in signal travel
time near companion

J1614-2230

most edge-on binary
pulsar known (89.17°)
+ massive white dwarf
companion (0.5 Msun)

heaviest neutron star
with 1.97 ± 0.04 Msun



Discovery of the heaviest neutron star (2013)

RESEARCH ARTICLE SUMMARY

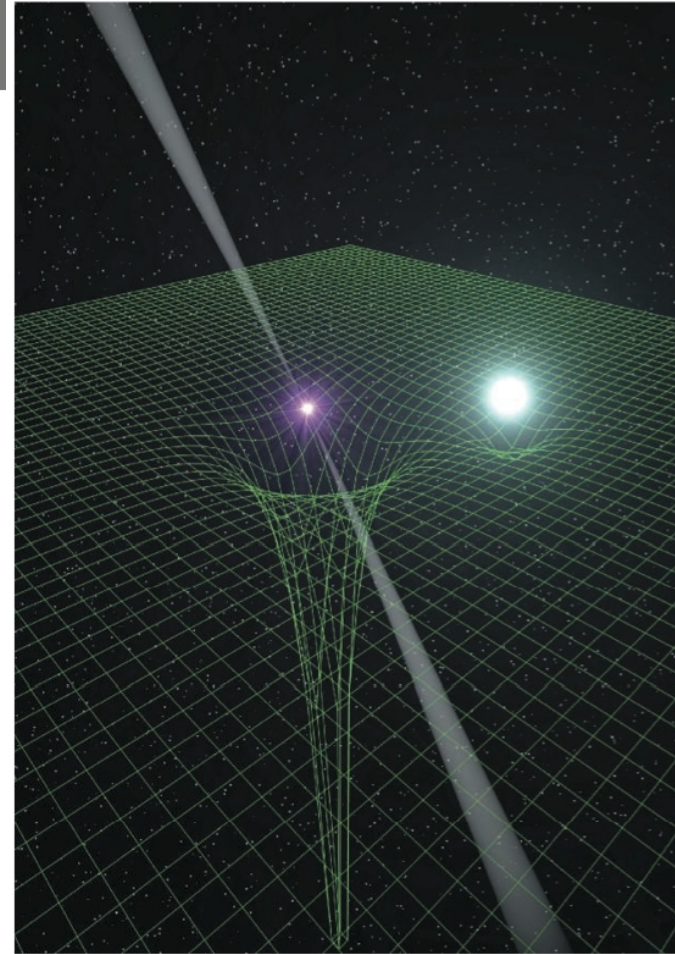
A Massive Pulsar in a Compact Relativistic Binary

John Antoniadis,* Paulo C. C. Freire, Norbert Wex, Thomas M. Tauris, Ryan S. Lynch, Marten H. van Kerkwijk, Michael Kramer, Cees Bassa, Vik S. Dhillon, Thomas Driebe, Jason W. T. Hessels, Victoria M. Kaspi, Vladislav I. Kondratiev, Norbert Langer, Thomas R. Marsh, Maura A. McLaughlin, Timothy T. Pennucci, Scott M. Ransom, Ingrid H. Stairs, Joeri van Leeuwen, Joris P. W. Verbiest, David G. Whelan

Introduction: Neutron stars with masses above $1.8 M_{\odot}$, possess extreme gravitational fields, which may give rise to phenomena outside general relativity. Hitherto, these strong-field deviations have not been probed by experiment, because they become observable only in tight binaries containing a high-mass pulsar and where orbital decay resulting from emission of gravitational waves can be tested. Understanding the origin of such a system would also help to answer fundamental questions of close-binary evolution.

Methods: We report on radio-timing observations of the pulsar J0348+0432 and phase-resolved optical spectroscopy of its white-dwarf companion, which is in a 2.46-hour orbit. We used these to derive the component masses and orbital parameters, infer the system's motion, and constrain its age.

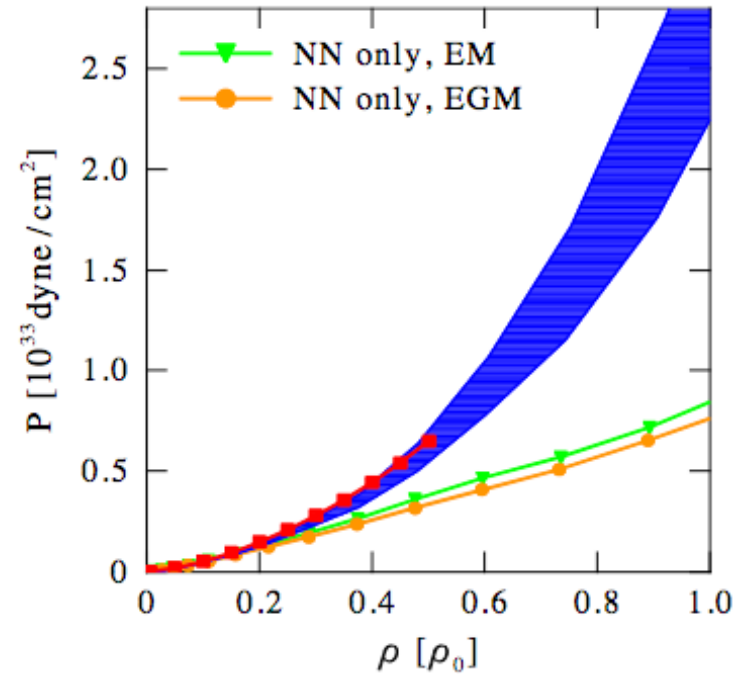
Results: We find that the white dwarf has a mass of $0.172 \pm 0.003 M_{\odot}$, which, combined with orbital velocity measurements, yields a pulsar mass of $2.01 \pm 0.04 M_{\odot}$. Additionally, over a span of 2 years, we observed a significant decrease in the orbital period, $\dot{P}_b^{\text{obs}} = -8.6 \pm 1.4 \mu\text{s year}^{-1}$ in our radio-timing data.



Artist's impression of the PSR J0348+0432 system. The compact pulsar (with beams of radio emission) produces a strong distortion of spacetime (illustrated by the green mesh). Conversely, spacetime around its white dwarf companion (in light blue) is substantially less curved. According to relativistic theories of gravity, the binary system is subject to energy loss by gravitational waves.

Impact on neutron stars Hebeler et al. (2010, 2013)

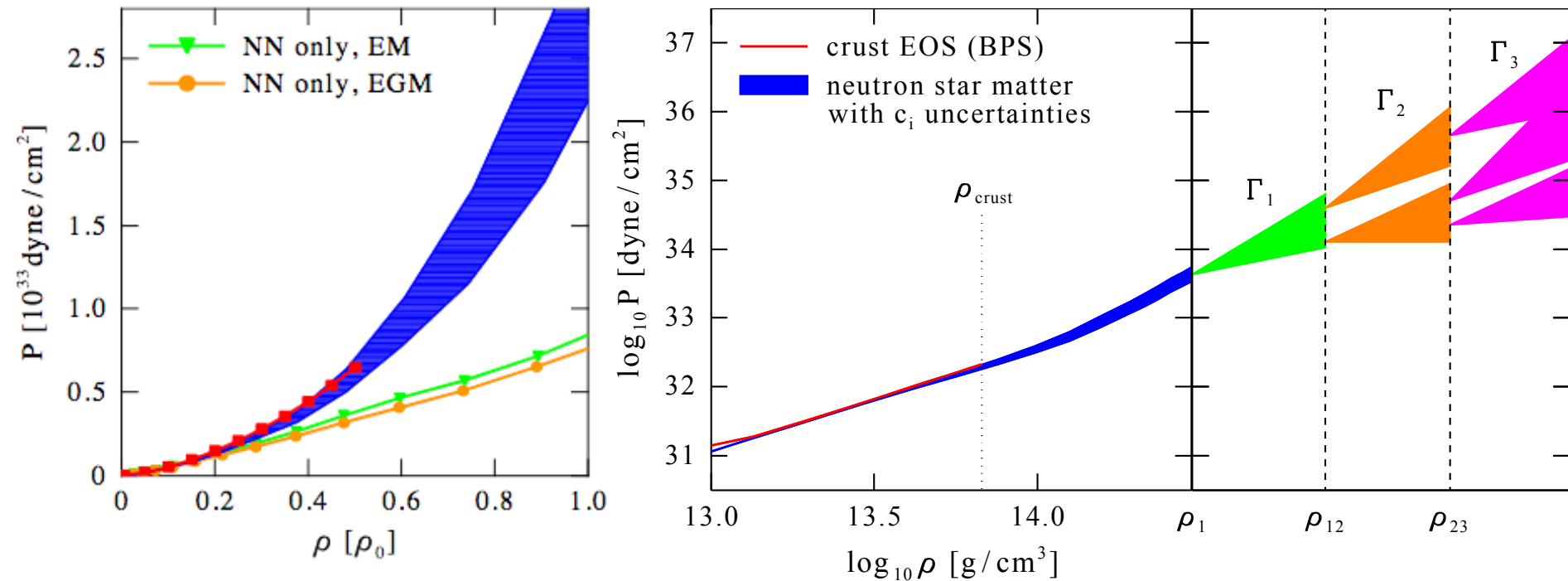
Equation of state/pressure for **neutron-star matter** (includes small Y_e, p)



pressure below nuclear densities agrees with standard crust equation of state only after 3N forces are included

Impact on neutron stars Hebeler et al. (2010, 2013)

Equation of state/pressure for **neutron-star matter** (includes small Y_e, p)



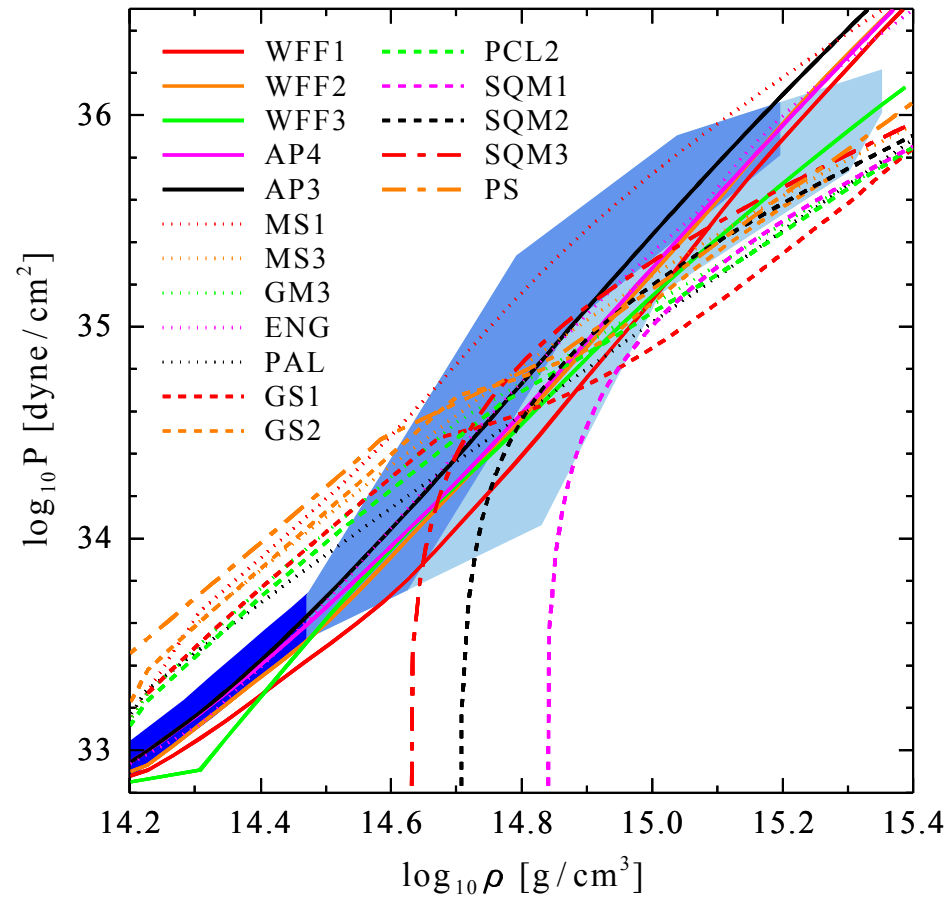
pressure below nuclear densities agrees with standard crust equation of state only after 3N forces are included

extend uncertainty band to higher densities using piecewise polytropes
allow for soft regions

Impact on neutron stars Hebeler et al. (2010, 2013)

constrain high-density EOS by causality, require to support 1.97 Msun star

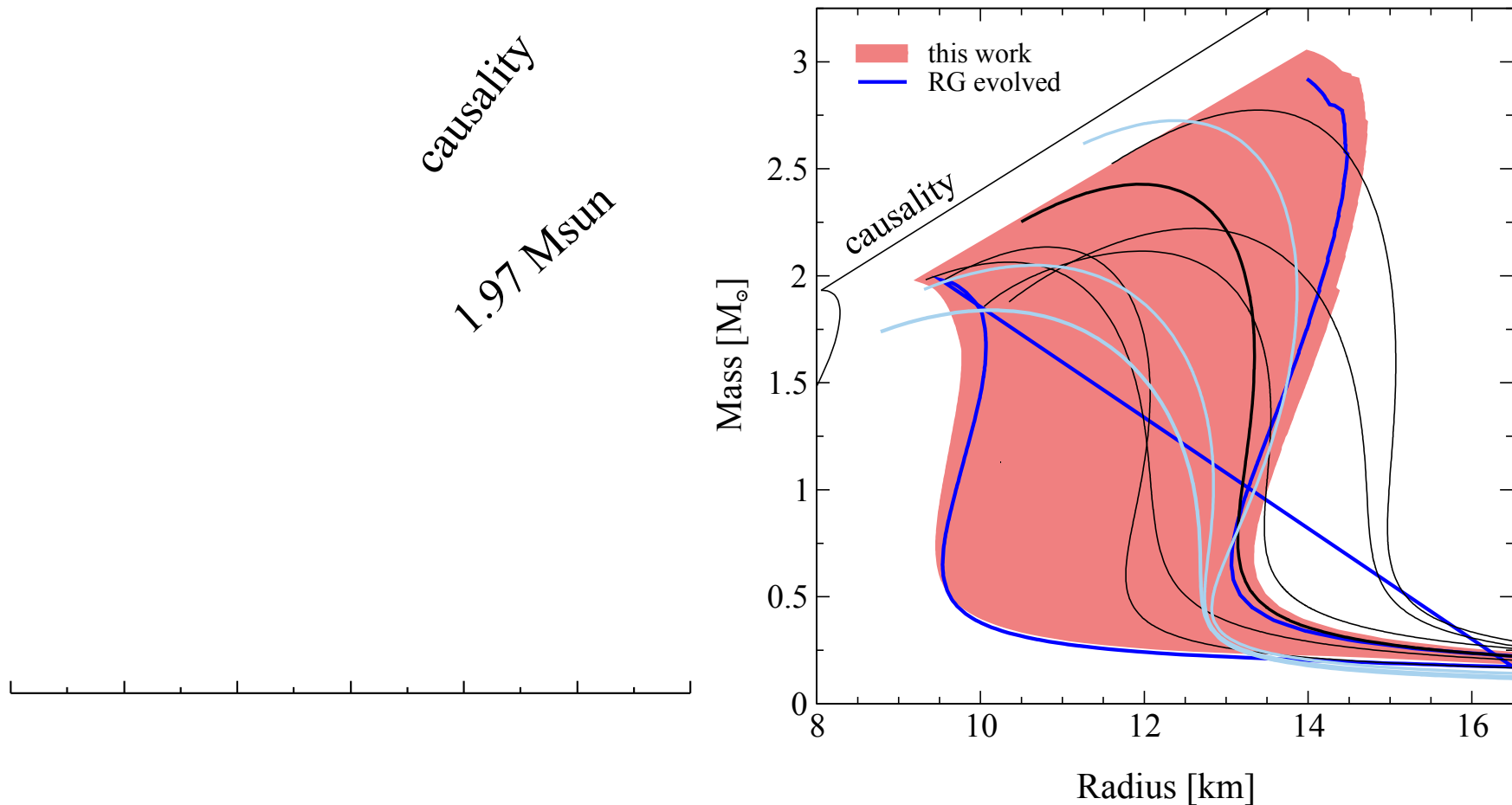
causality
1.97 Msun



low-density pressure sets scale, chiral EFT interactions provide strong constraints, ruling out many model equations of state

Impact on neutron stars Hebeler et al. (2010, 2013)

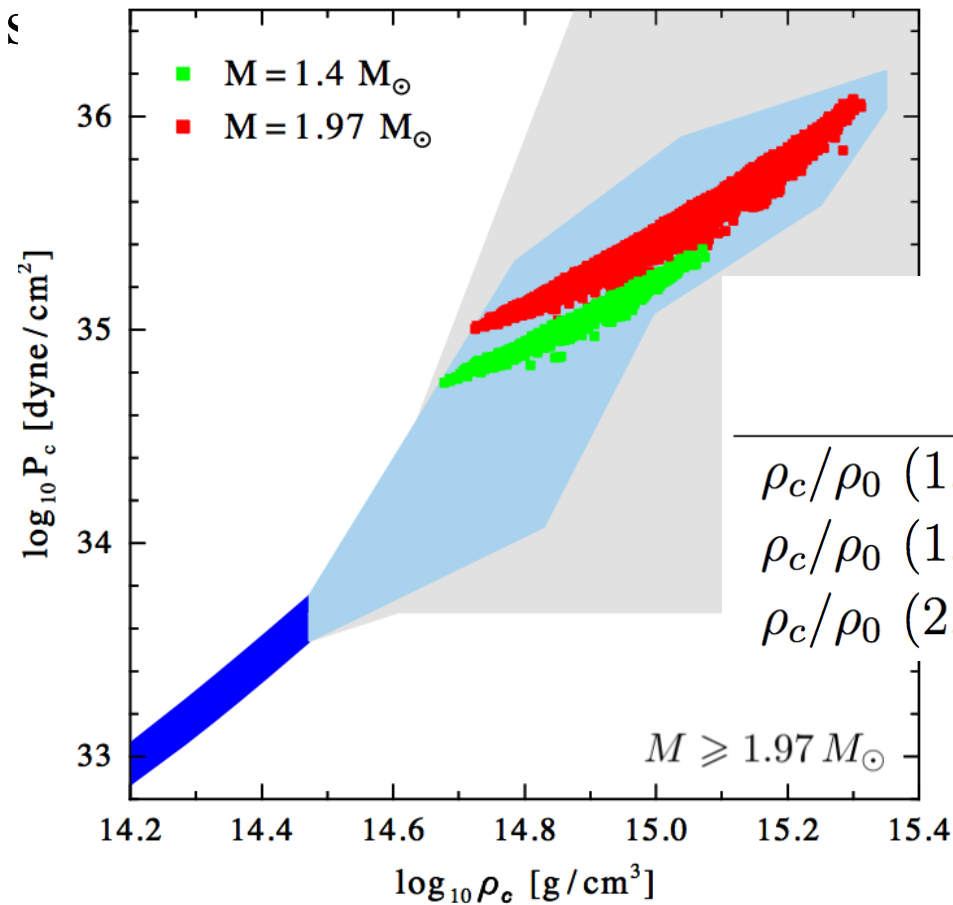
constrain high-density EOS by causality, require to support 1.97 Msun star



low-density pressure sets scale, chiral EFT interactions provide strong constraints, ruling out many model equations of state

Impact on neutron stars Hebeler et al. (2010, 2013)

constrain high-density EOS by causality, require to support 1.97 Msun



	$\widehat{M} = 1.97 M_{\odot}$		$\widehat{M} = 2.4 M_{\odot}$	
	min	max	min	max
$\rho_c/\rho_0 (1.4 M_{\odot})$	1.8	4.4	1.8	2.7
$\rho_c/\rho_0 (1.97 M_{\odot})$	2.0	7.6	2.0	3.4
$\rho_c/\rho_0 (2.4 M_{\odot})$			2.2	5.4

low-density pressure sets scale, chiral EFT interactions provide strong constraints, ruling out many model equations of state

Neutron star mergers and gravitational waves

Neutron-star mergers and gravitational waves

explore sensitivity to neutron-rich matter in neutron-star merger and gw signal

Bauswein, Janka (2012), Bauswein, Janka, Hebeler, AS (2012).

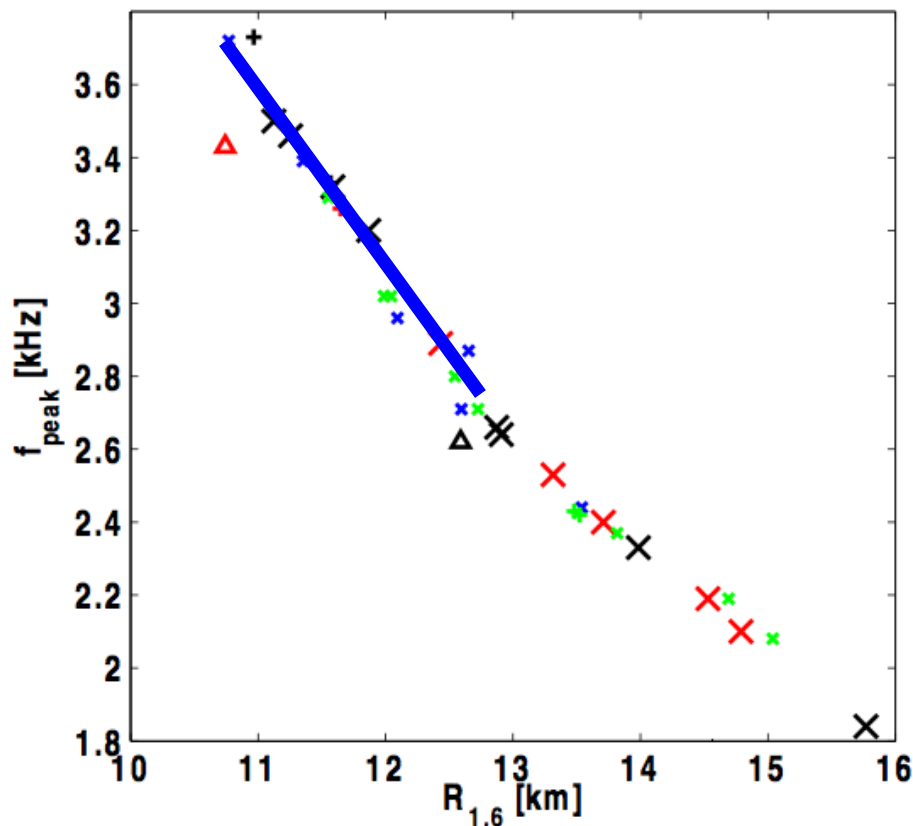


FIG. 10: Peak frequency of the postmerger GW emission versus the radius of a nonrotating NS with $1.6 M_{\odot}$ for different EoSs. Symbols have the same meaning as in Fig. 8.

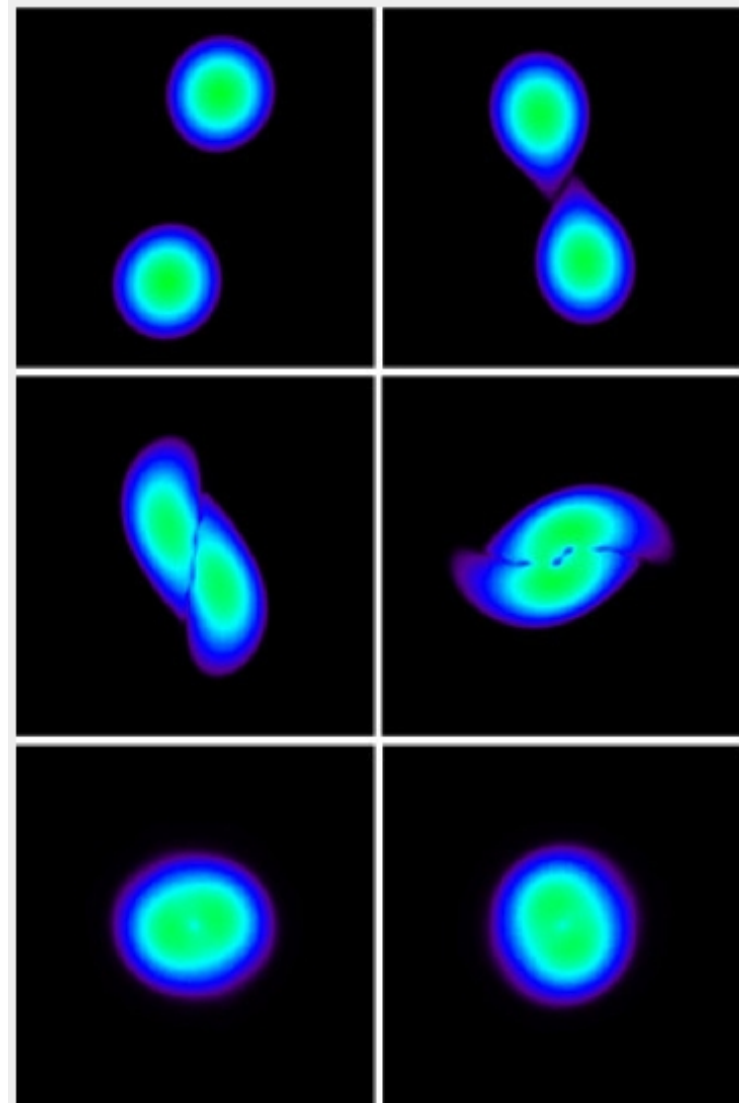


Fig. 1: Various snapshots of the collision of two neutron stars initially revolving around each other. The sequence simulated by the computer covers only 0.03 seconds. The two stars orbit each other counterclockwise (top left) and quickly come closer (top right). Finally they collide (centre left), merge (centre right), and form a dense, superheavy neutron star (bottom). Strong vibrations of the collision remnant are noticeable as deformations in east-west direction and in north-south direction (bottom panels). (Simulation: Andreas Bauswein and H.-Thomas Janka/MPA)

Direct dark matter detection

WIMP scattering off nuclei needs **nuclear structure factors** as input

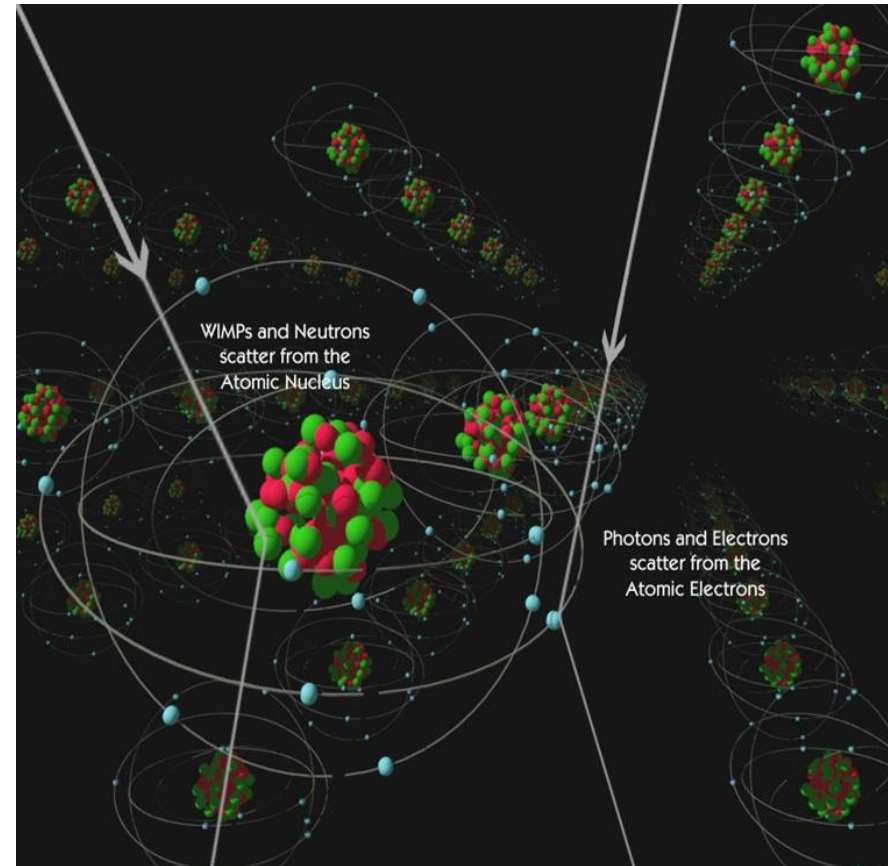
particularly sensitive to nuclear physics for **spin-dependent** couplings

relevant momentum transfers $\sim m\pi$

**calculate systematically
with chiral effective field theory**

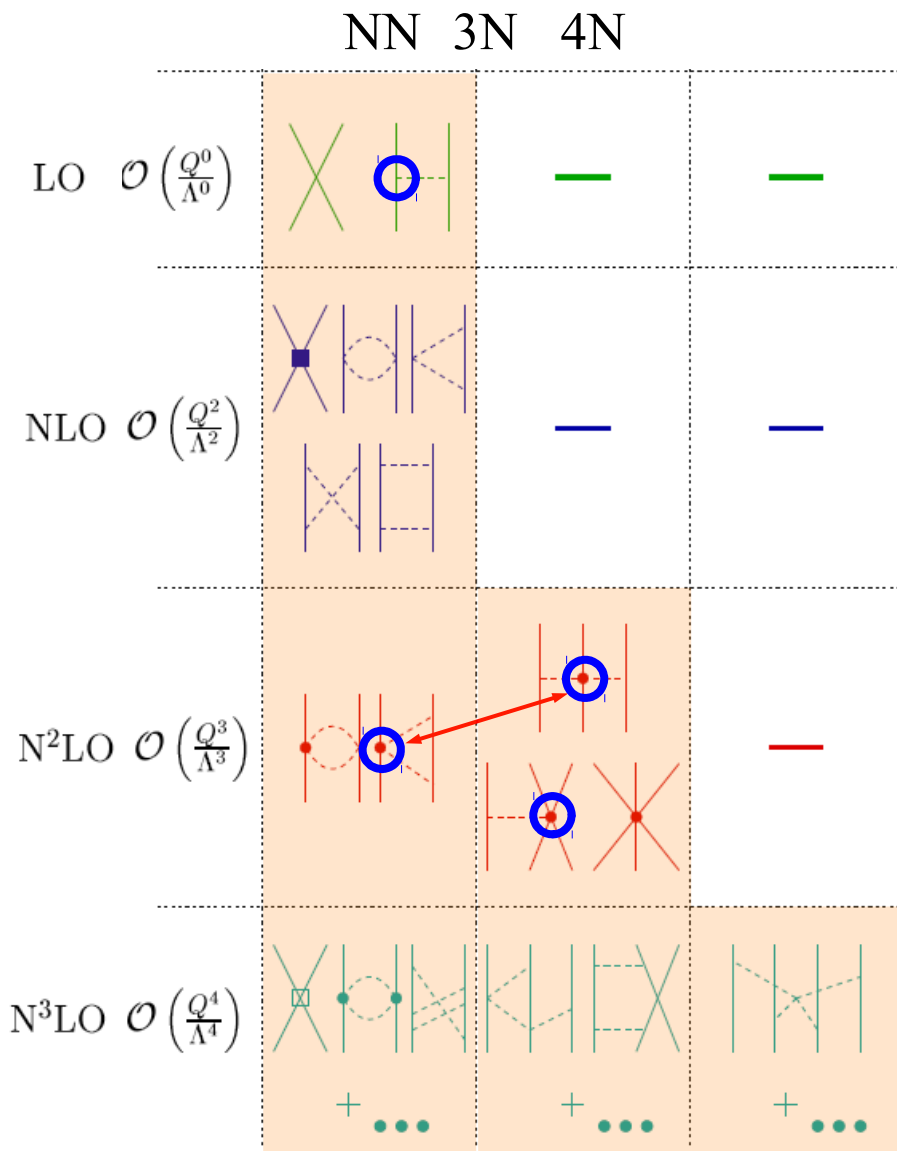
Menendez, Gazit, AS (2012),

Klos, Menendez, Gazit, AS (2013)

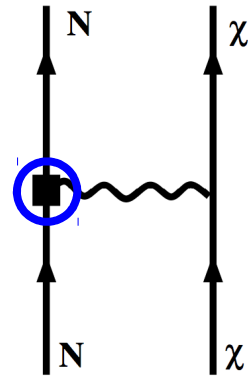


from CDMS collaboration

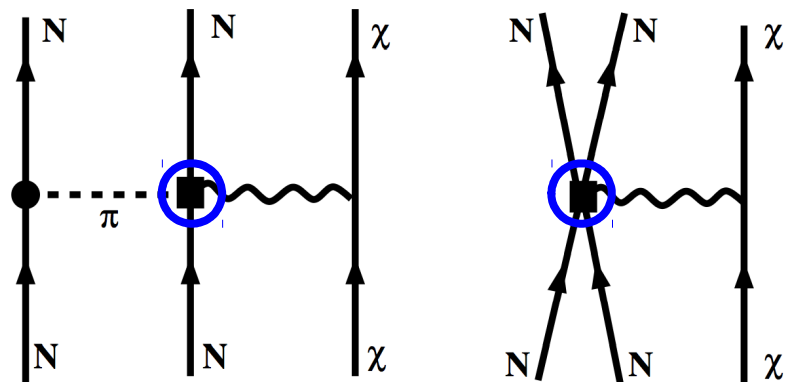
Chiral EFT for WIMP currents in nuclei



one-body currents at Q0 and Q2

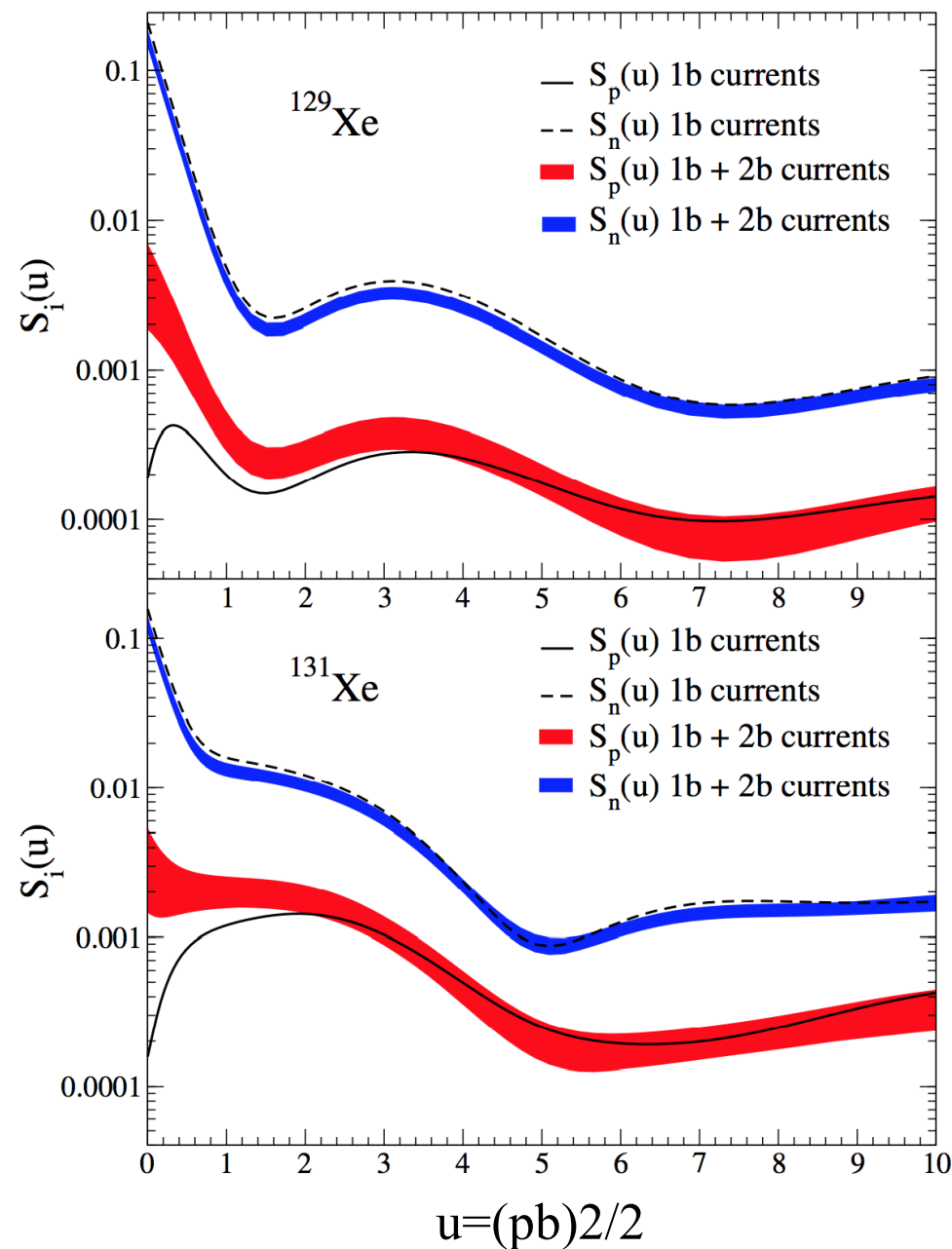


+ two-body currents at Q3

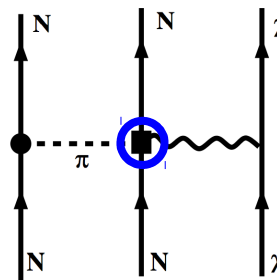


same couplings in forces and currents!

Xenon response with 1+2-body currents



two-body currents due to strong interactions among nucleons



WIMPs couple to neutrons and protons at the same time

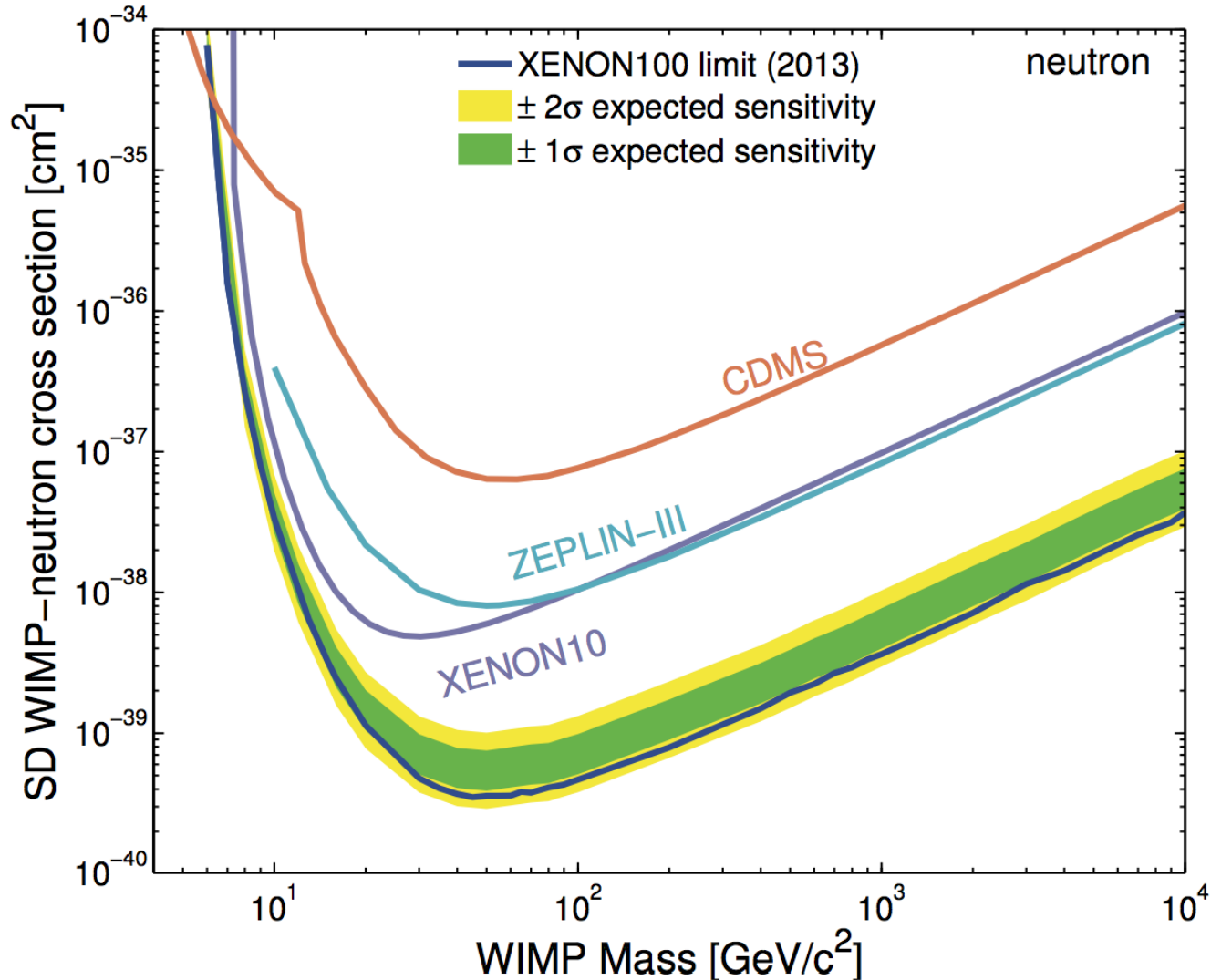
enhances coupling to even species in all cases

first calculations with chiral EFT currents and state-of-the-art nuclear interactions

Limits on SD WIMP-neutron interactions

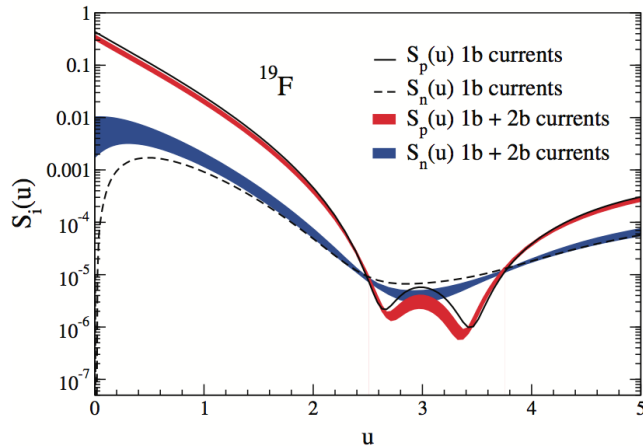
best limits from XENON100 *Aprile et al. (2013)*

used our calculations with uncertainty bands for WIMP currents in nuclei

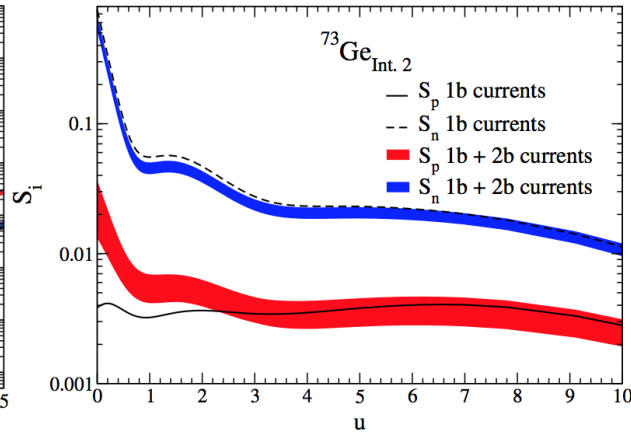


Spin-dependent WIMP-nucleus response for ^{19}F , ^{23}Na , ^{27}Al , ^{29}Si , ^{73}Ge , ^{127}I

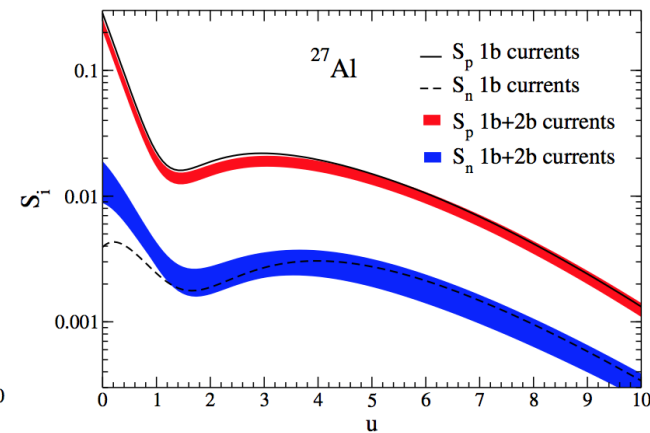
Klos, Menendez, Gazit, AS (2013)



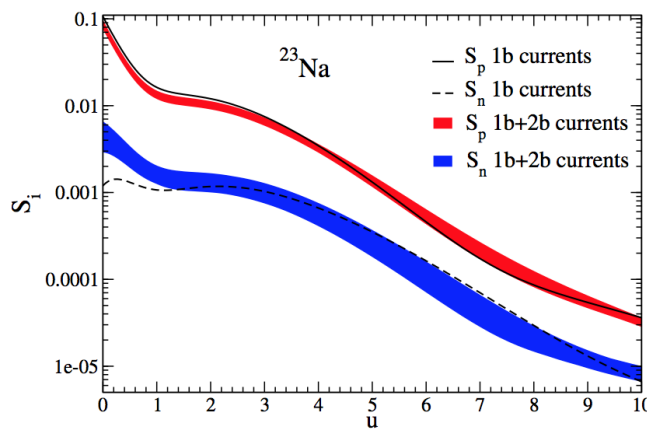
PICASSO, COUPP, SIMPLE



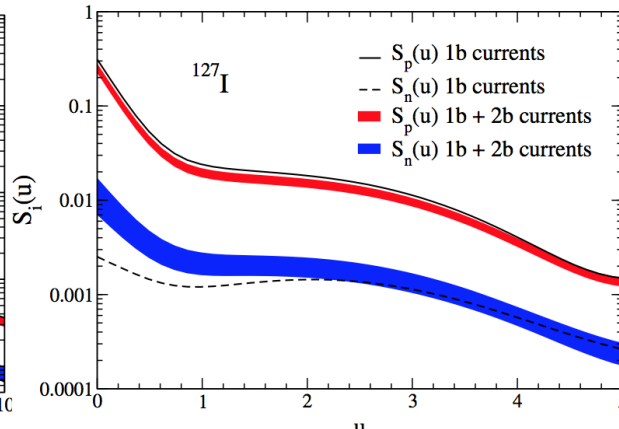
CDMS, EDELWEISS, EURECA



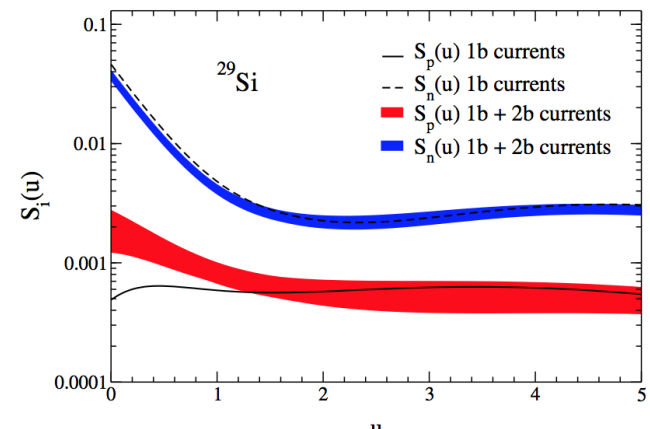
CRESST



DAMA, ANAIS, DM-Ice



DAMA, ANAIS, DM-Ice, KIMS

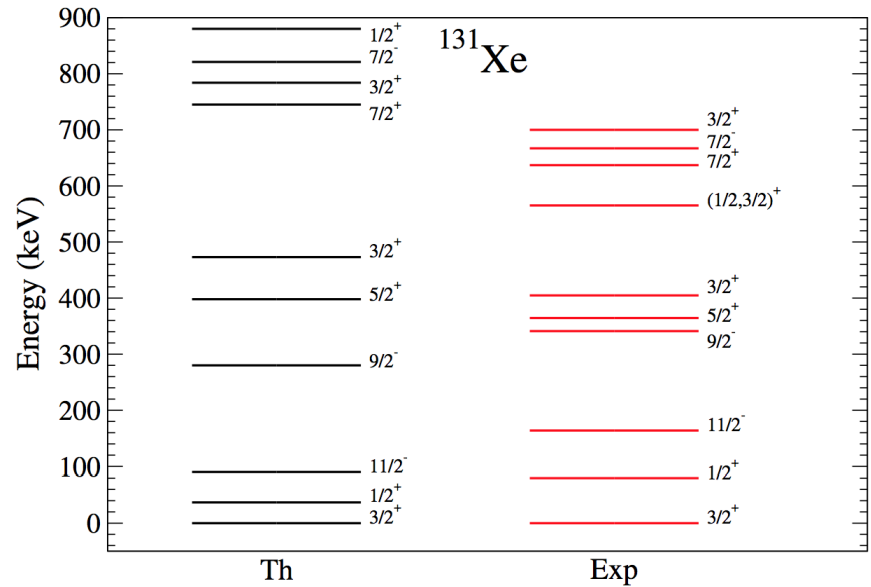
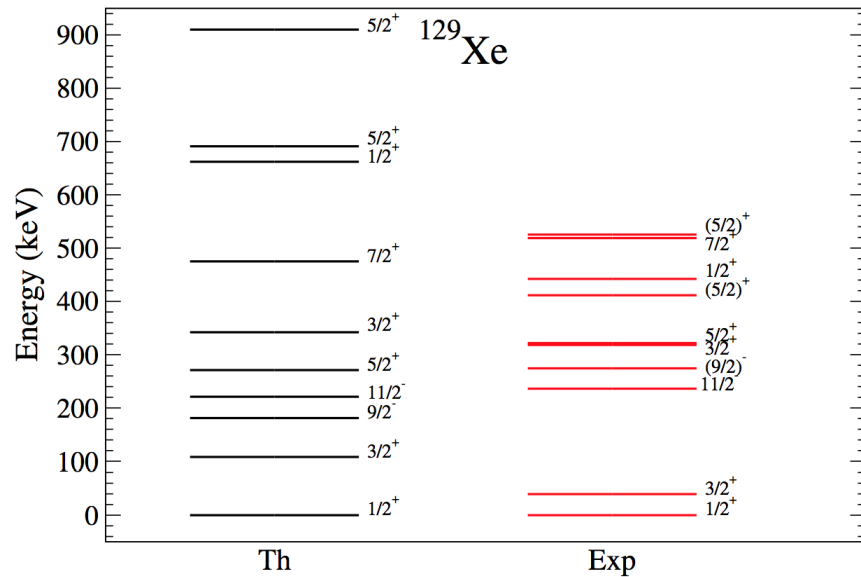


CDMS-II

Nuclear structure for direct detection

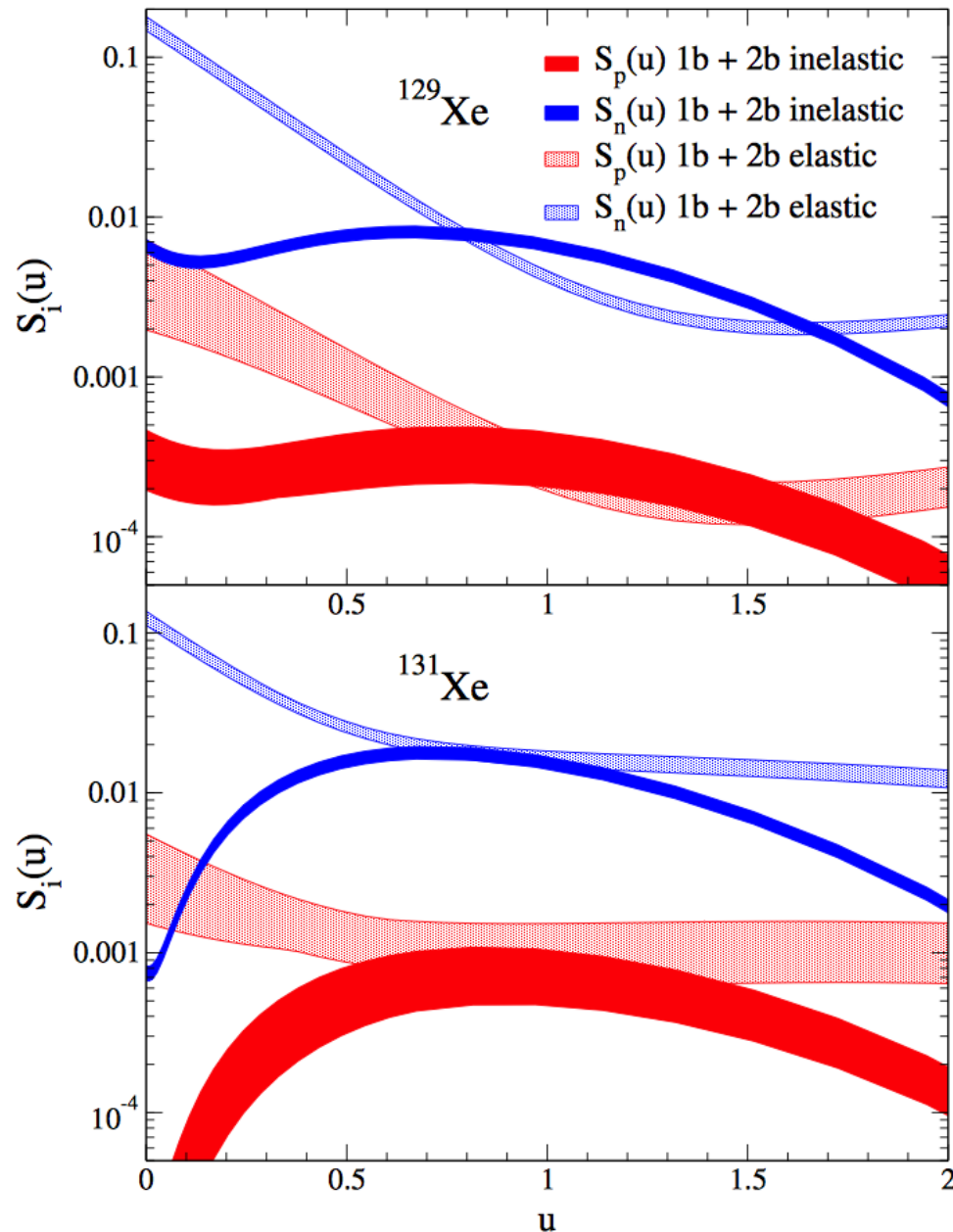
valence-shell Hamiltonian calculated from NN interactions + corrections to compensate for not including 3N forces (will improve in the future)

valence spaces and interactions have been tested successfully in nuclear structure calculations, largest spaces used



Inelastic WIMP scattering to 40 and 80 keV excited states

Baudis, Kessler, Klos, Lang, Menendez, Reichard, AS, arXiv:1309.0825

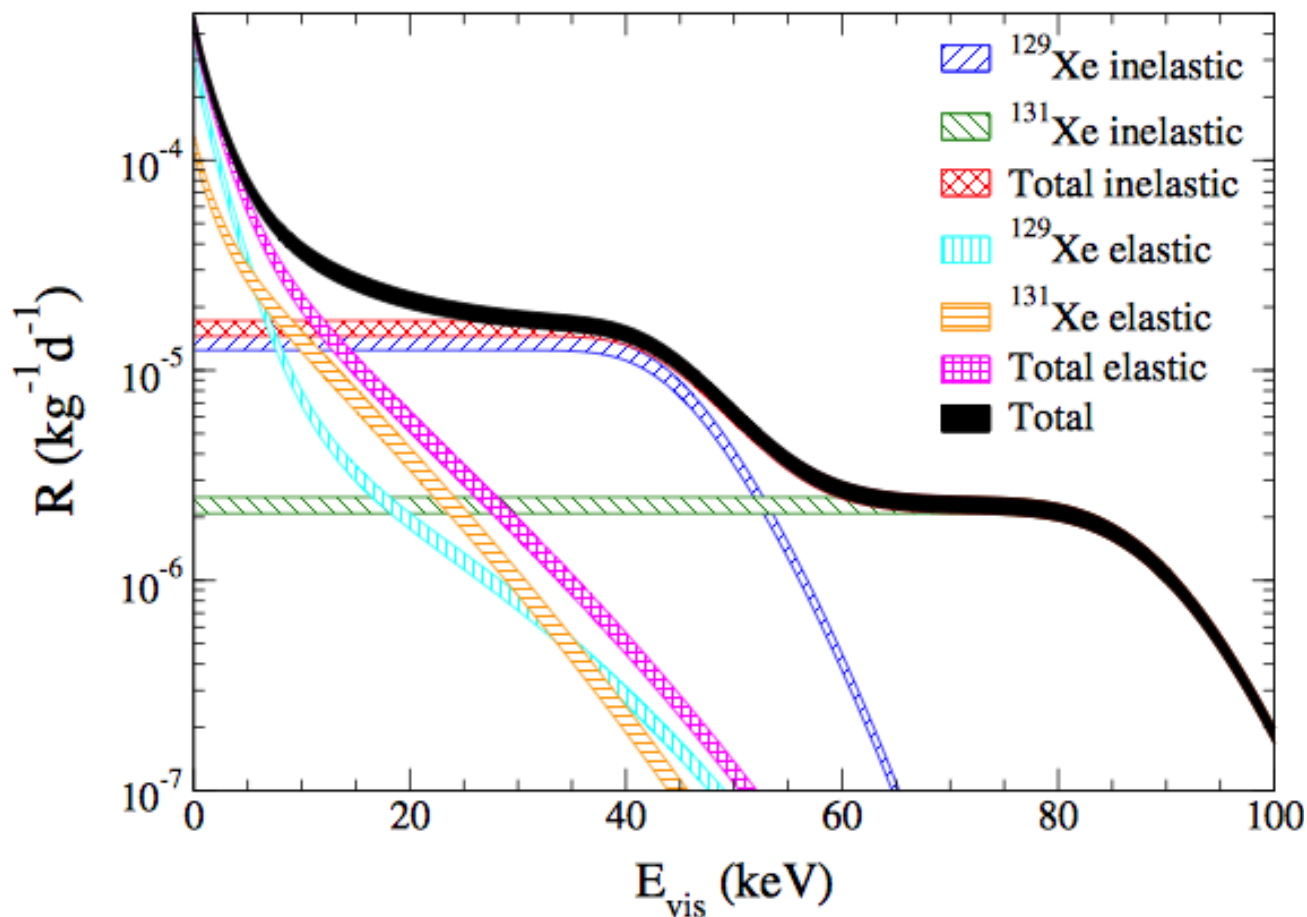


inelastic channel
comparable/dominates elastic
channel for
 $p \sim 150 \text{ MeV}$

Signatures for **inelastic** WIMP scattering

elastic recoil + **prompt γ from de-excitation**

combined information from elastic and inelastic channel will allow to **determine dominant interaction channel** in one experiment

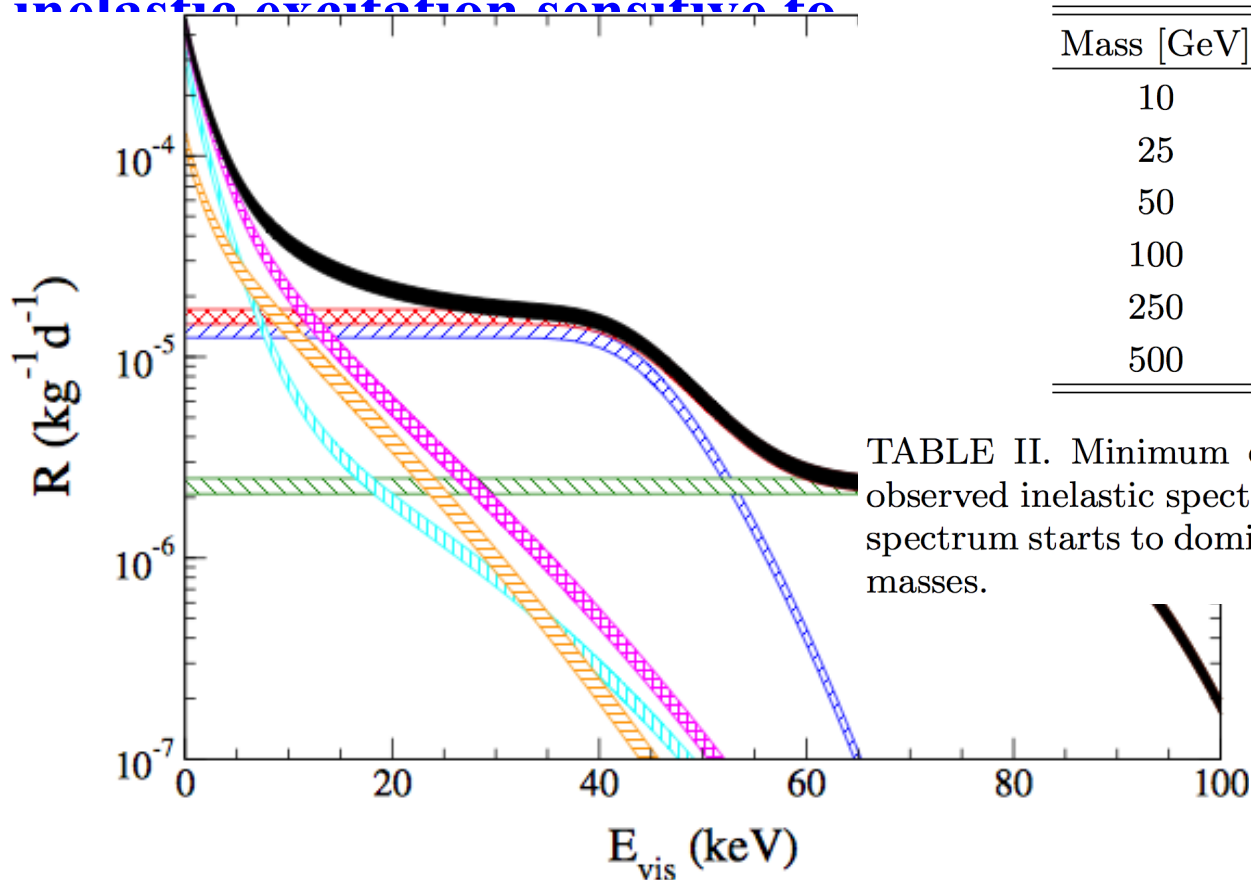


Signatures for **inelastic** WIMP scattering

elastic recoil + prompt γ from de-excitation

combined information from elastic and inelastic channel will allow to **determine dominant interaction channel** in one experiment

inelastic excitation sensitive to WIMP



Mass [GeV]	^{129}Xe	^{131}Xe	Total
10	—	—	—
25	5	—	5
50	7	17	9
100	7	24	12
250	9	32	19
500	11	35	24

TABLE II. Minimum energy E_{vis} in keV above which the observed inelastic spectrum for ^{129}Xe , ^{131}Xe and for the total spectrum starts to dominate the elastic one for various WIMP masses.

Summary

3N forces are a frontier

in chiral EFT, for neutron-rich nuclei, matter, and neutron stars

key for **neutron-rich nuclei**: O, Ca isotopes, N=28 and shell evolution

J.D. Holt, J. Menéndez, T. Otsuka, J. Simonis, T. Suzuki

dominant uncertainty of **neutron (rich) matter** below nuclear densities

predicts **neutron skin** with theoretical uncertainty comparable to exp.

constrains **neutron star radii and equation of state** for astrophysics

C. Drischler, K. Hebeler, T. Krüger, V. Soma, I. Tews, J.M. Lattimer, C.J. Pethick

dark matter response of nuclei and two-body currents

J. Menéndez, P. Klos, D. Gazit

Thank you very much!

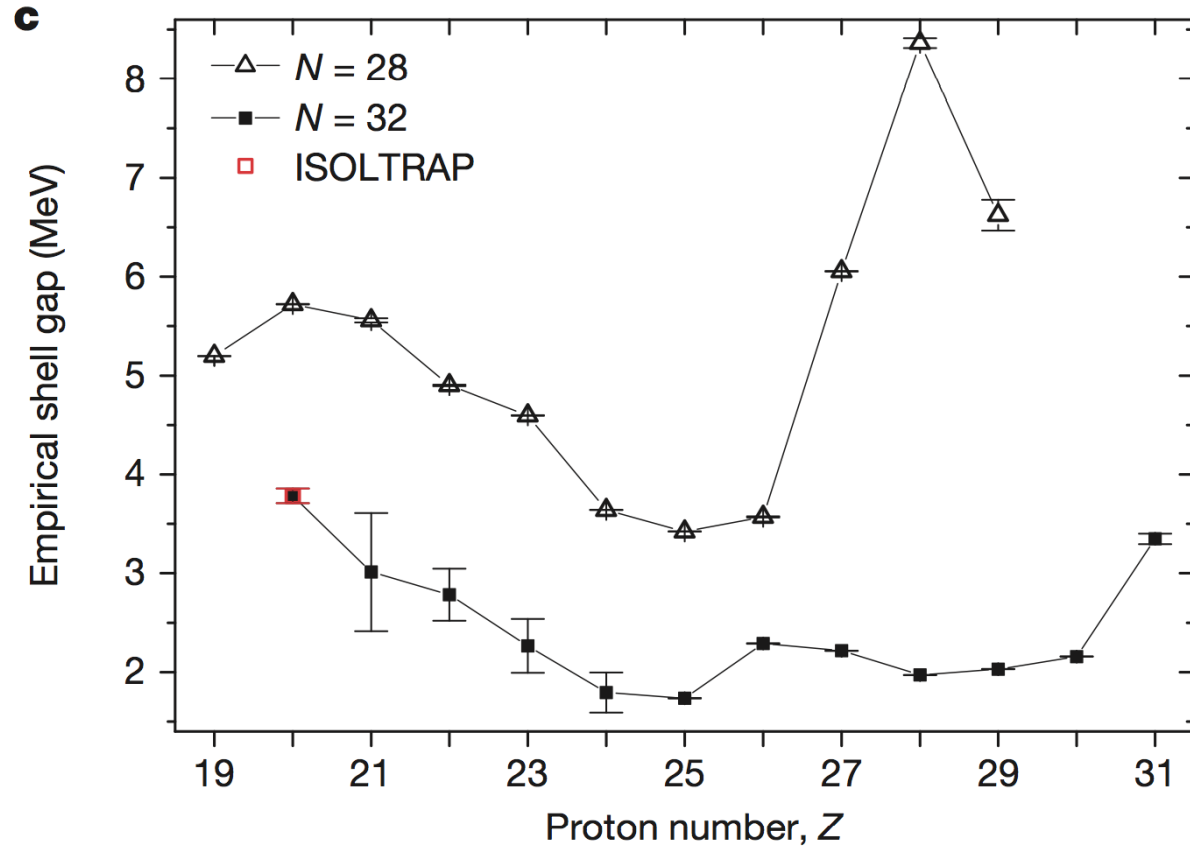
Masses of exotic calcium isotopes pin down nuclear forces

F. Wienholtz¹, D. Beck², K. Blaum³, Ch. Borgmann³, M. Breitenfeldt⁴, R. B. Cakirli^{3,5}, S. George¹, F. Herfurth², J. D. Holt^{6,7}, M. Kowalska⁸, S. Kreim^{3,8}, D. Lunney⁹, V. Manea⁹, J. Menéndez^{6,7}, D. Neidherr², M. Rosenbusch¹, L. Schweikhard¹, A. Schwenk^{7,6}, J. Simonis^{6,7}, J. Stanja¹⁰, R. N. Wolf¹ & K. Zuber¹⁰

shell gap of 4 MeV

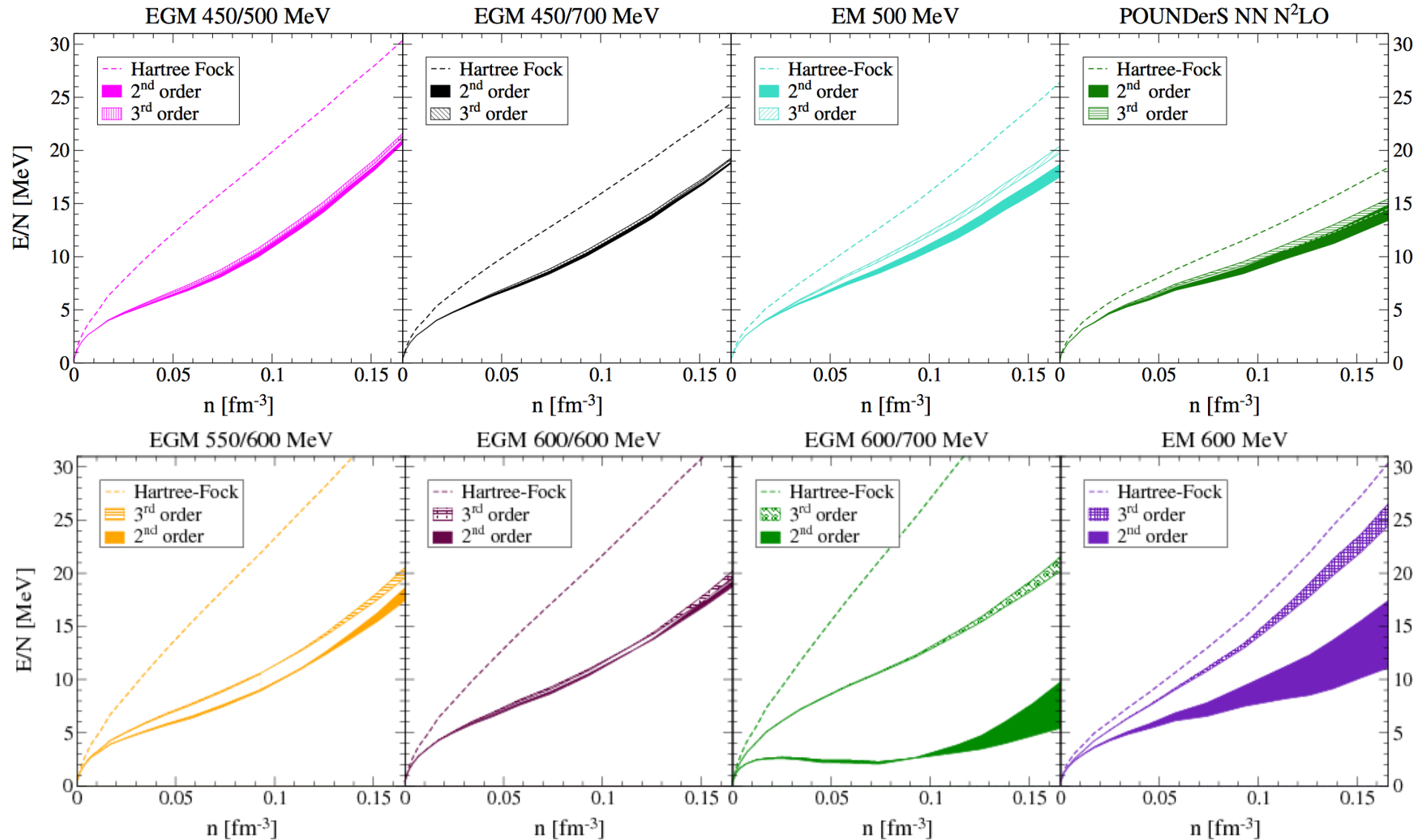
evolution to $Z=20$

similar for $N=28$ and 32



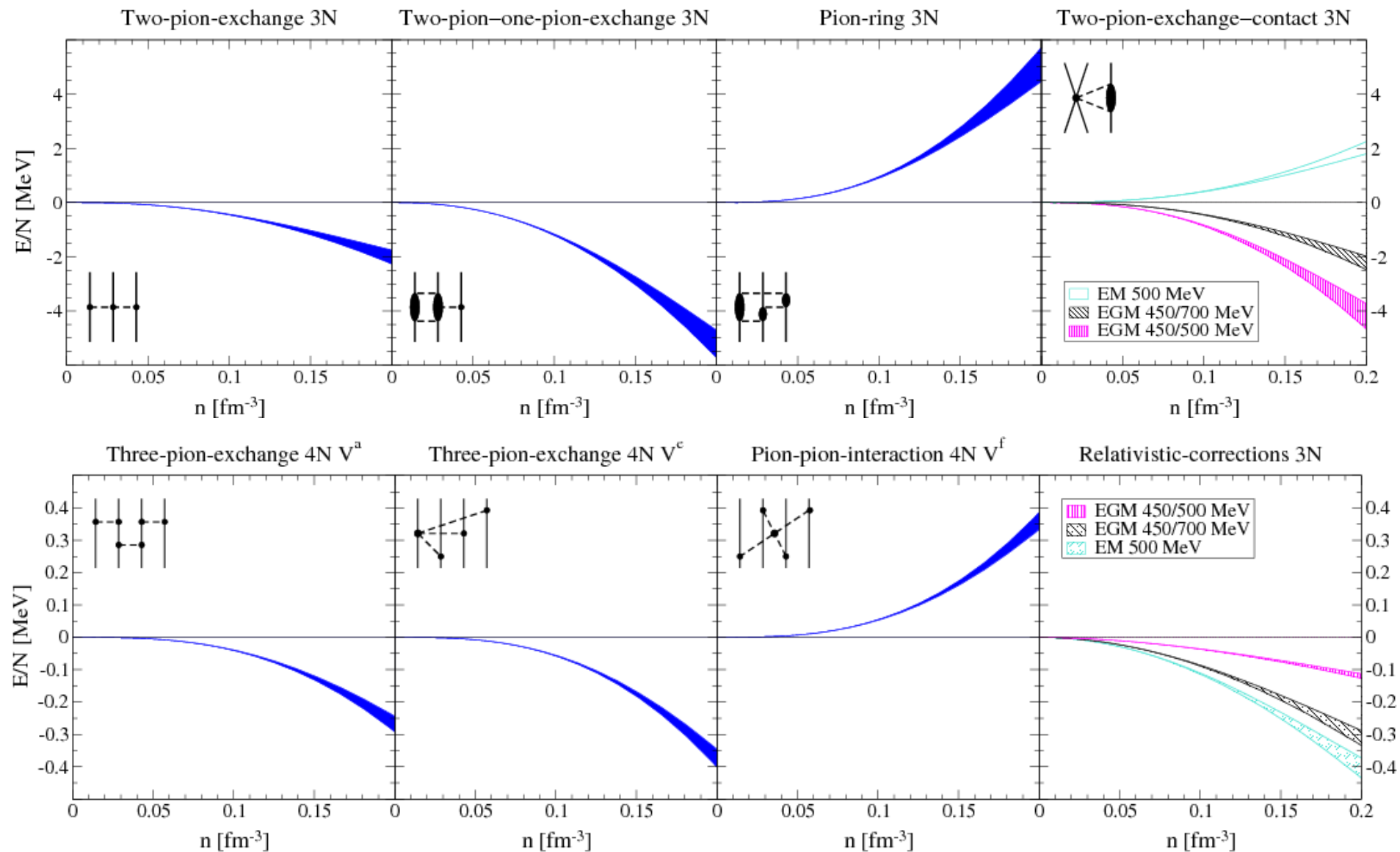
Neutron matter from chiral EFT interactions

direct calculations without RG/SRG evolution, 3N to N²LO only



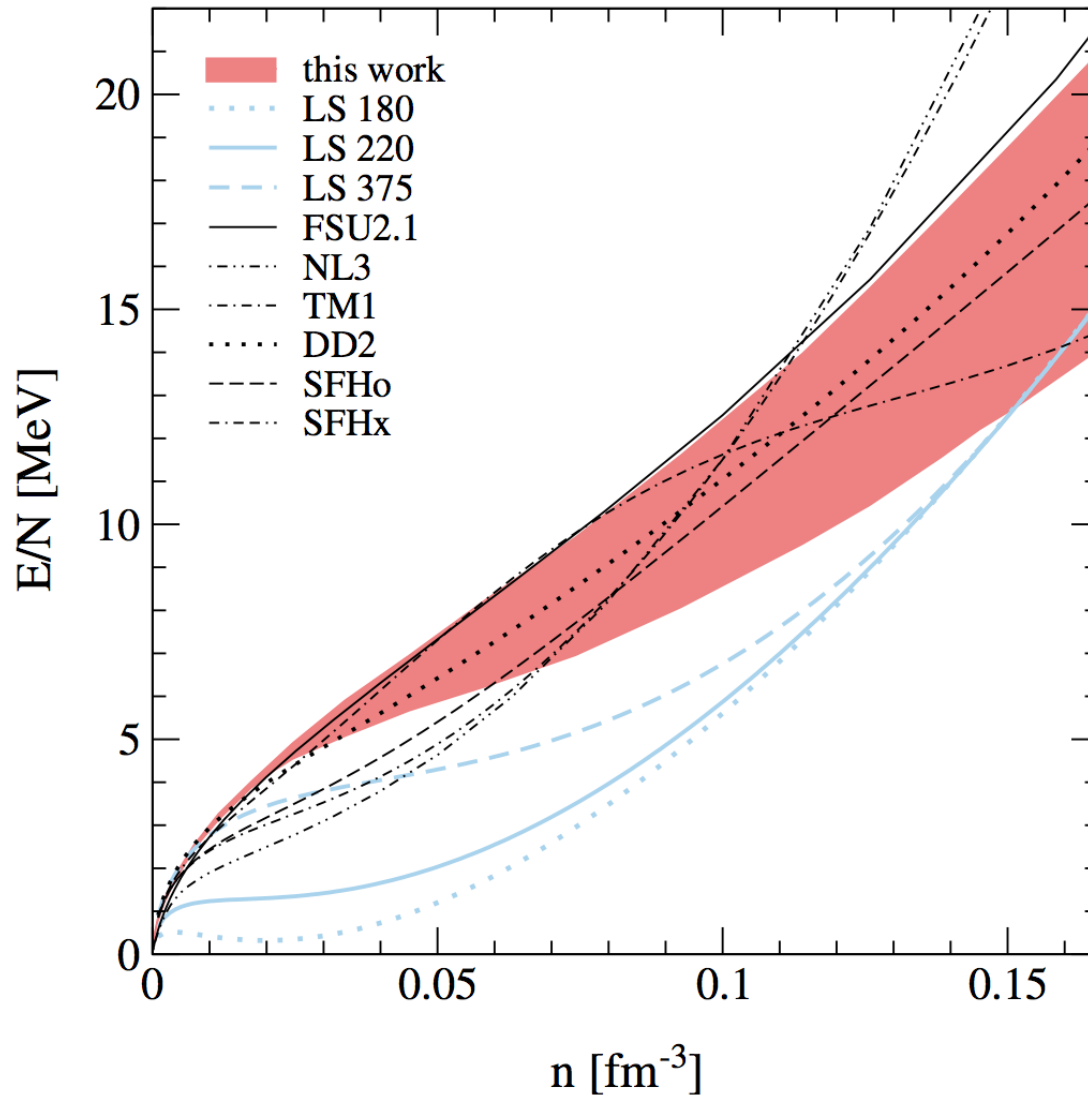
N3LO 3N and 4N interactions in neutron matter

evaluated at Hartree-Fock level



Comparisons to equations of state in astrophysics

many equations of state used in supernova simulations not consistent with neutron matter results



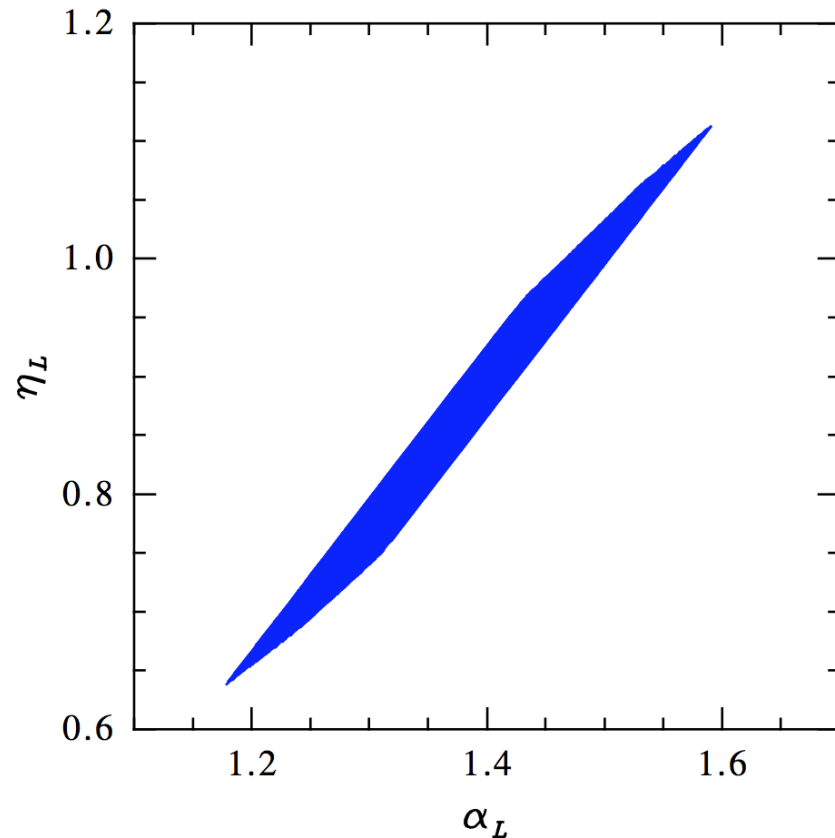
Symmetry energy and density derivative L

extract using empirical parametrization [Hebeler, Lattimer, Pethick, AS \(2013\)](#)

$$\begin{aligned} \frac{E(\bar{n}, x)}{A} = T_0 & \left[\frac{3}{5} \left(x^{\frac{5}{3}} + (1-x)^{\frac{5}{3}} \right) (2\bar{n})^{\frac{2}{3}} \right. \\ & - \left((2\alpha - 4\alpha_L) x (1-x) + \alpha_L \right) \bar{n} \\ & \left. + \left((2\eta - 4\eta_L) x (1-x) + \eta_L \right) \bar{n}^\gamma \right] \end{aligned}$$

expansion in Fermi momentum ($\gamma=4/3$),
kinetic energy + quadratic asymmetry

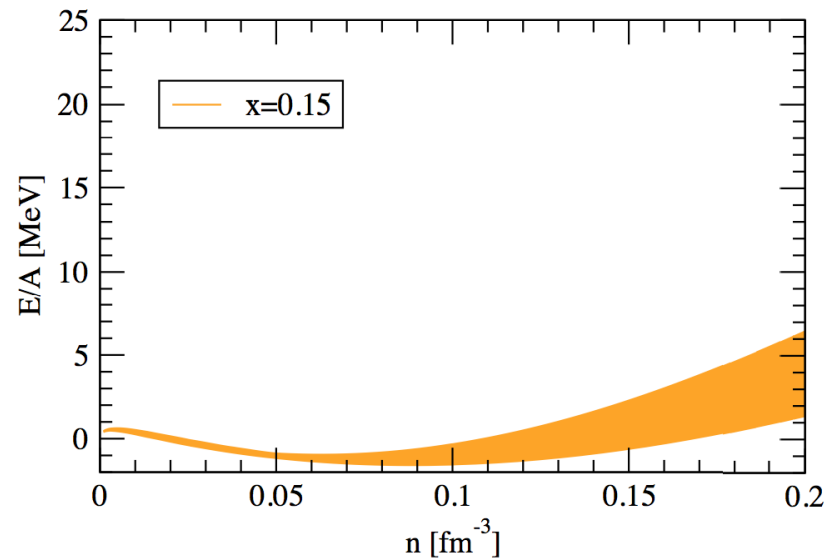
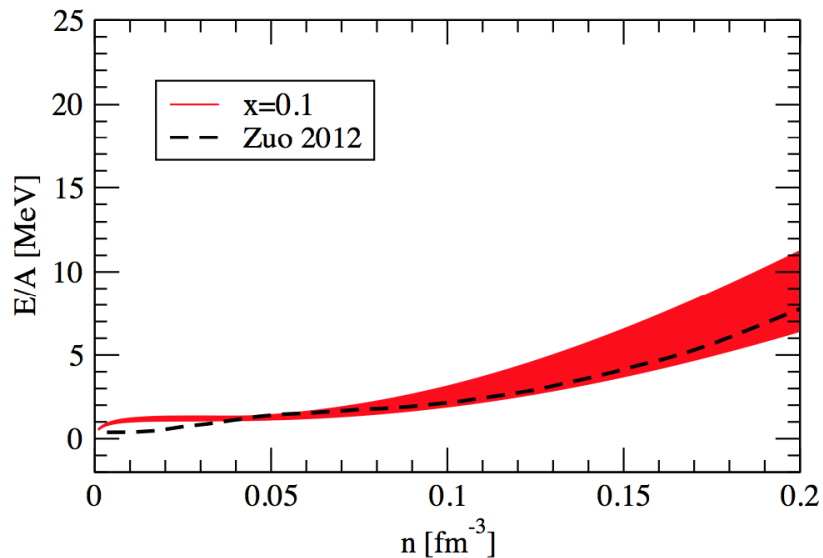
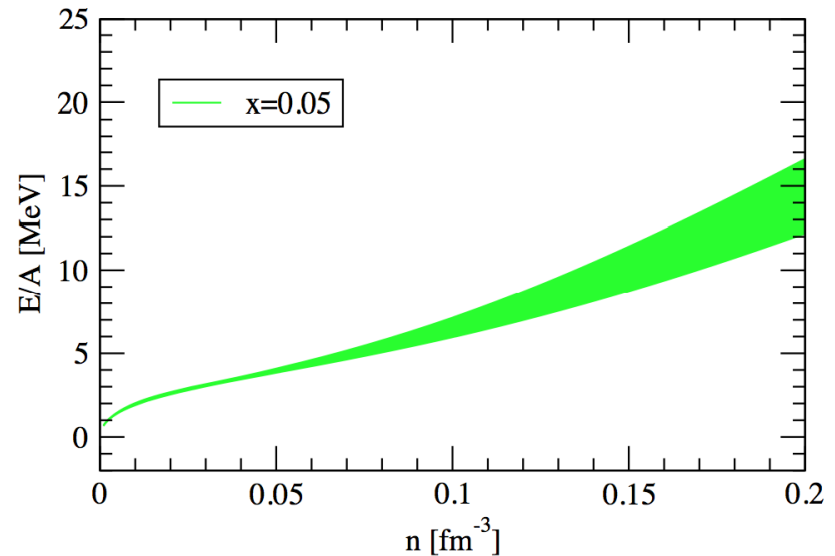
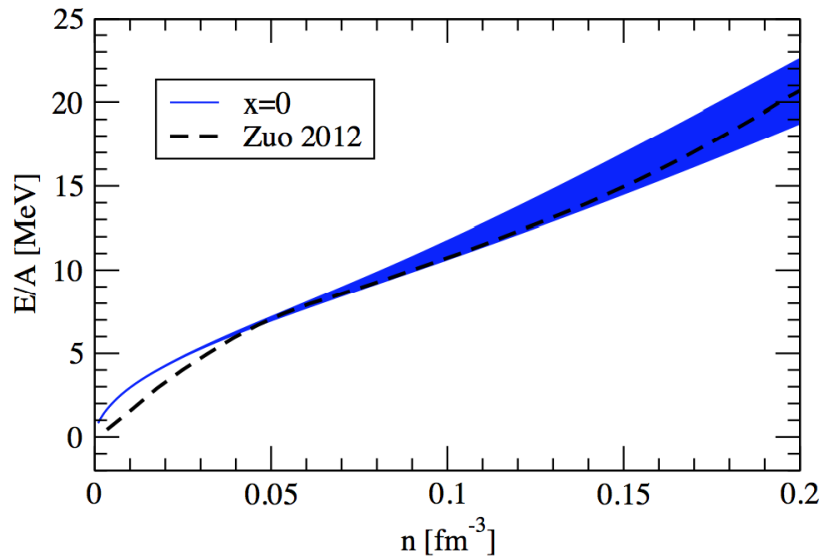
α, η fit to empirical saturation point
 α_L, η_L fit to neutron matter calculations



Ab-initio calculations of asymmetric matter

based on N3LO NN + N2LO 3N interactions [Drischler, Soma, AS \(2013\)](#)

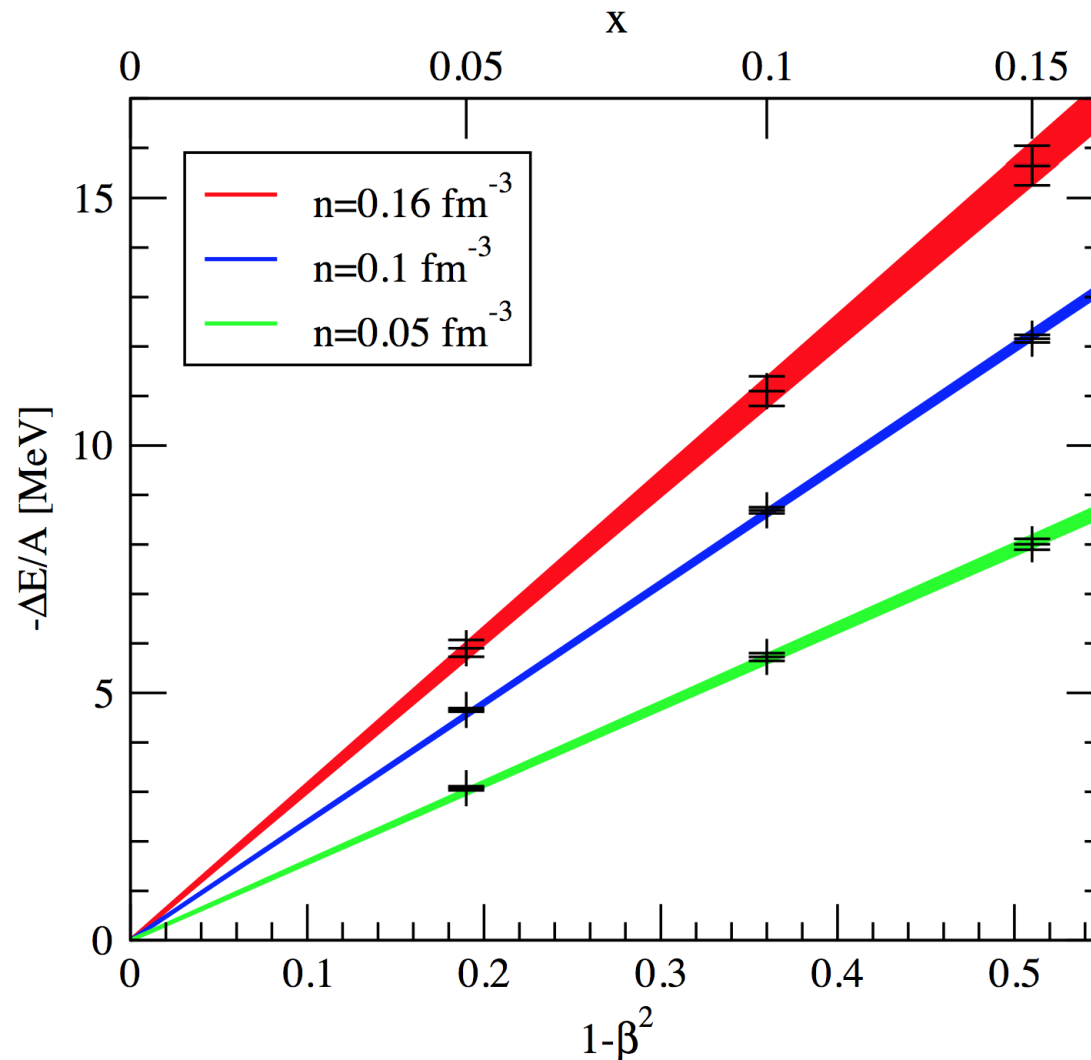
uncertainty band dominated by 3N



Ab-initio calculations of asymmetric matter

compares well with quadratic expansion even for n-rich conditions

$$\frac{E(n, \beta)}{A} = \frac{E(n, \beta = 0)}{A} + E_{\text{sym}}(n) \beta^2 + \mathcal{O}(\beta^4)$$

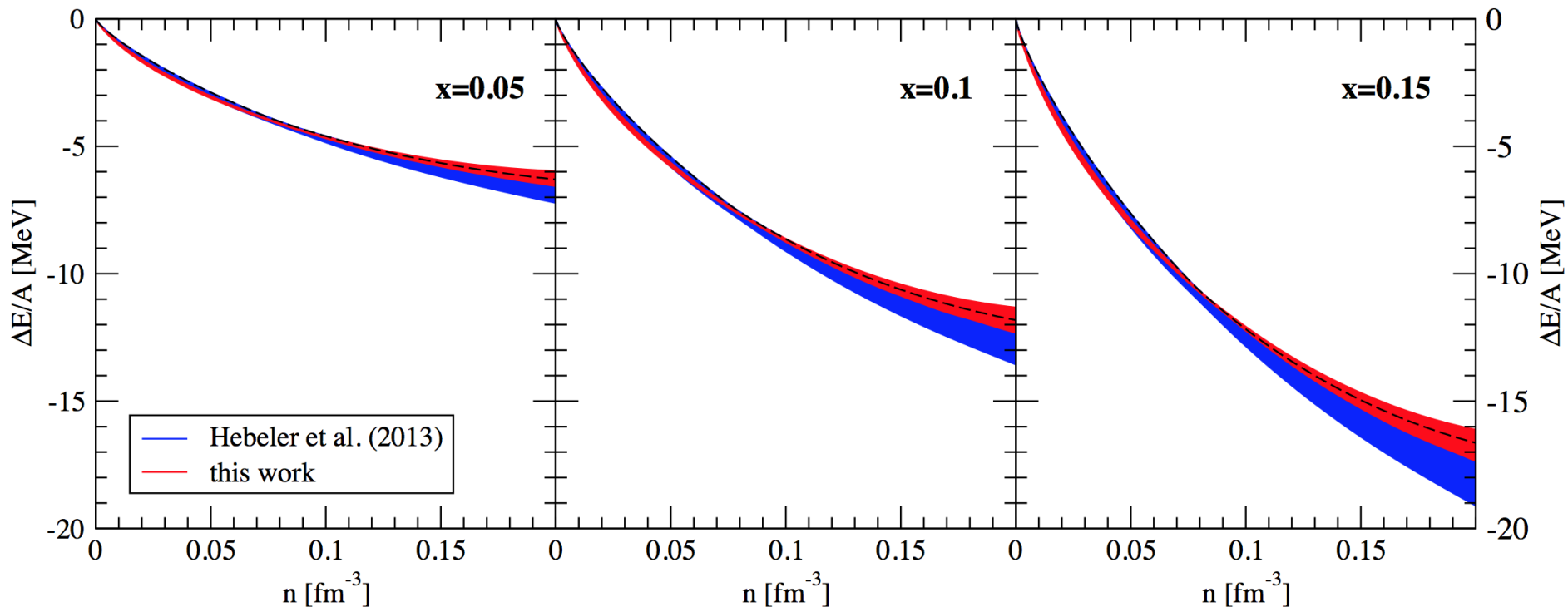


Ab-initio calculations of asymmetric matter

benchmark empirical parametrization: $\Delta E = \text{diff. to neutron matter}$

good agreement with ab-initio calculations, very useful for astrophysics

$$\frac{E(\bar{n}, x)}{A} = T_0 \left[\frac{3}{5} \left(x^{\frac{5}{3}} + (1-x)^{\frac{5}{3}} \right) (2\bar{n})^{\frac{2}{3}} \right. \\ \left. - ((2\alpha - 4\alpha_L) x (1-x) + \alpha_L) \bar{n} \right. \\ \left. + ((2\eta - 4\eta_L) x (1-x) + \eta_L) \bar{n}^\gamma \right]$$

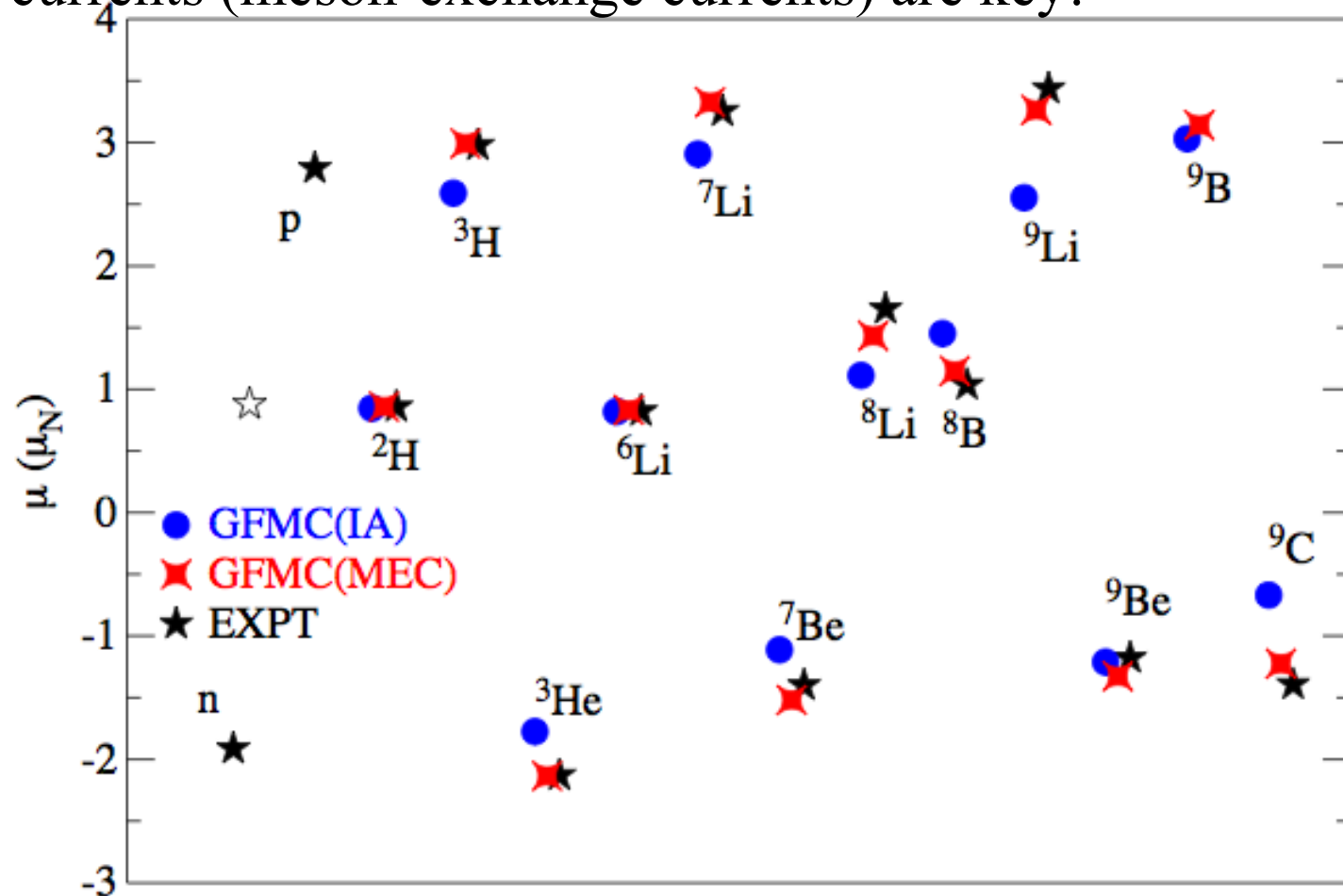


Chiral EFT currents and electroweak interactions

predicts consistent 1- and 2-body currents

GFMC calculations of magnetic moments in light nuclei [Pastore et al. \(2012\)](#)

2-body currents (meson-exchange currents) are key!

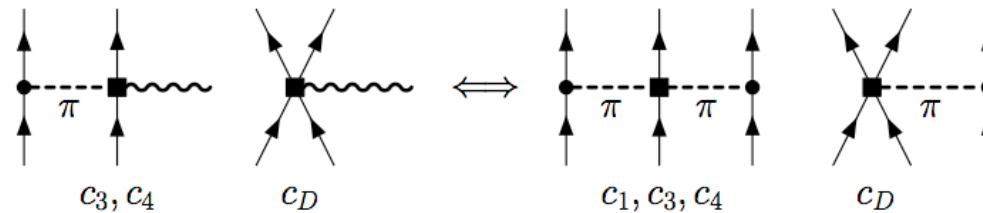


Electroweak interactions and 3N forces

weak axial currents couple to spin, similar to pions

two-body currents predicted by NN, 3N couplings to N3LO

Park et al., Phillips,...



two-body analogue of Goldberger-Treiman relation

explored in light nuclei, but not for larger systems

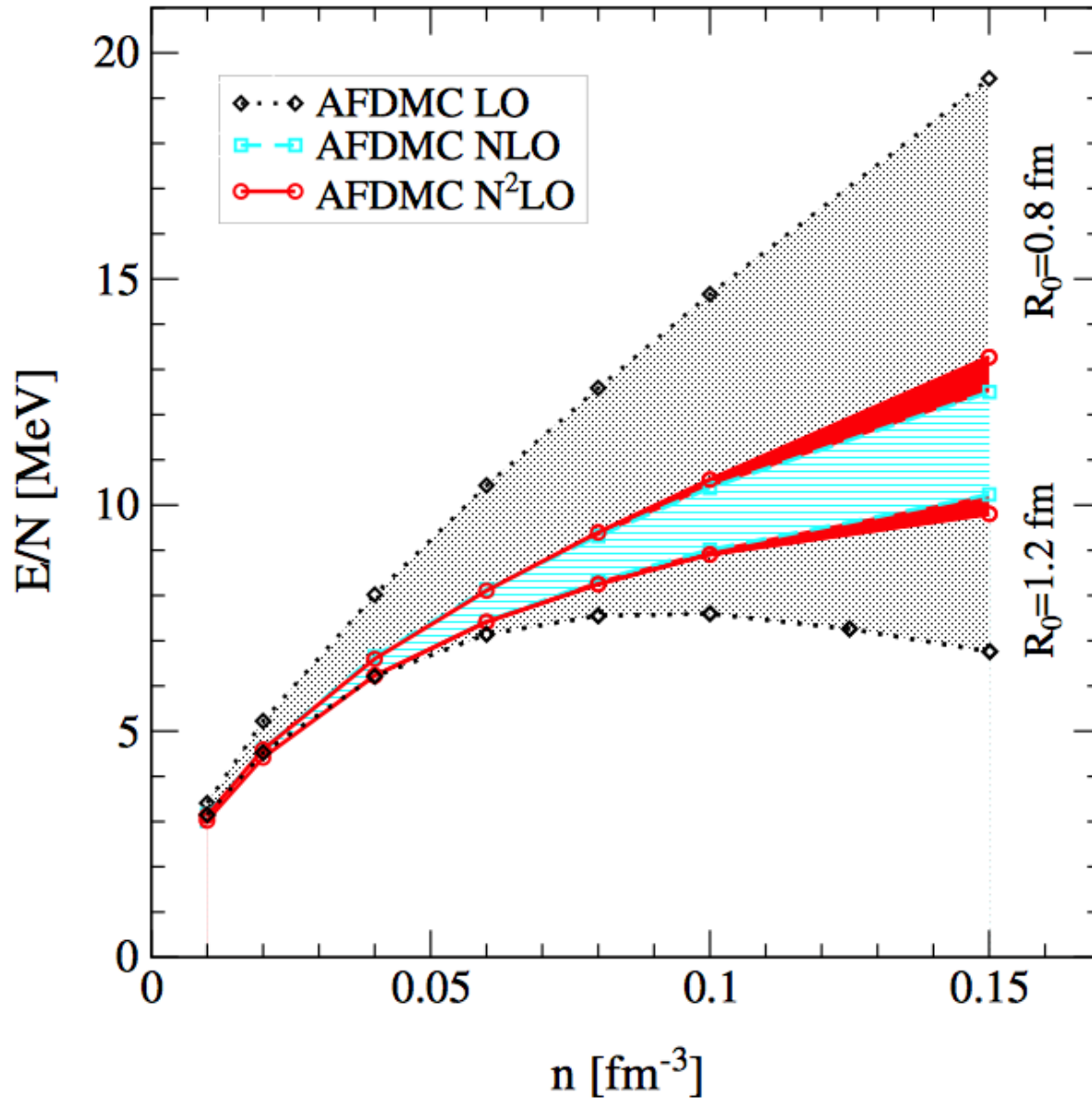
dominant contribution to Gamow-Teller transitions,
important in nuclei ($Q \sim 100$ MeV)

3N couplings predict quenching of g_A (dominated by long-range part)
and predict momentum dependence (weaker quenching for larger p)

Menendez, Gazit, AS (2011)

AFDMC results for neutron matter

order-by-order convergence up to saturation density

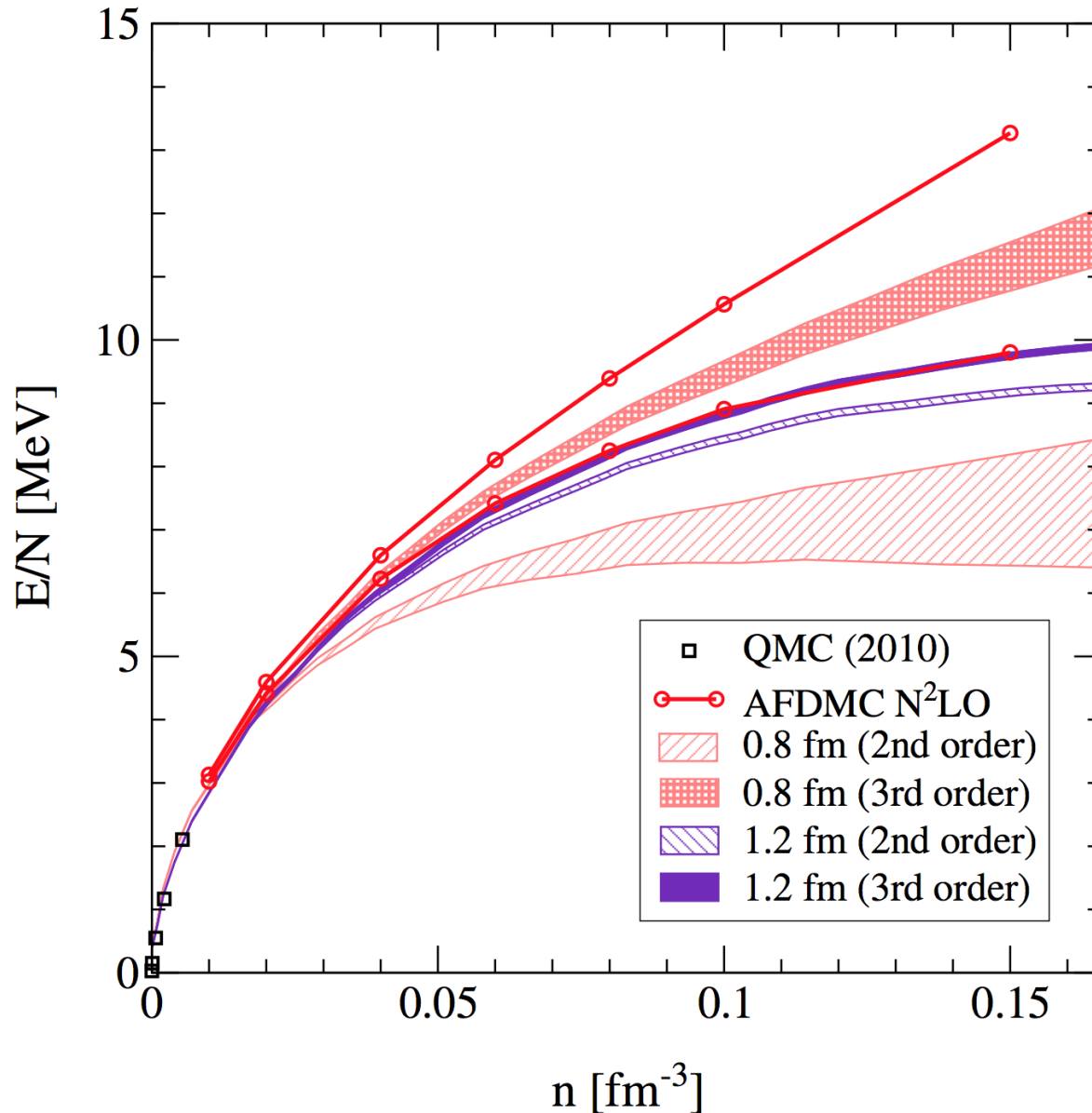


bands similar to
phase shift bands

NLO \sim N2LO
due to large c_i

Comparison to perturbative calculations at N2LO

Hartree-Fock +2nd order +3rd order (pp+hh), same as for N3LO calcs.



band at each order from
free to HF spectrum

low cutoffs (400 MeV)
3rd order corr. small,
excellent agreement
with AFDMC